

SELF ASSESSMENT TEST -3

CLASS 10+2

log function exponential form

1. Diff. x^x w.r.t.x

2. Diff. $(\cos x)^x + x^{\cos x}$ w.r.t.x

3. If $y = \sqrt{\tan x + \sqrt{\tan x + \sqrt{\tan x + \dots \infty}}}$ prove $\frac{dy}{dx} = \frac{\sec^2 x}{2y-1}$

4. If $x^y + y^x = 5$ find $\frac{dy}{dx}$

5. If $x^5 y^4 = (x+y)^9$ prove that $\frac{dy}{dx} = \frac{y}{x}$

6. Find $\frac{dy}{dx}$ when $xy = e^{x-y}$

7. If $(\sin x)^y = (\cos y)^x$ find $\frac{dy}{dx}$

8. If $y = (\sin x)^{(\sin x)^{(\sin x)^{\dots \infty}}}$ prove $\frac{dy}{dx} = \frac{y^2 \cot x}{1 - y \log \sin x}$

9. Diff. $\sqrt{\frac{(x-1)(x-2)}{(x-3)(x-4)(x-5)}}$ w.r.t.x

10. If $x = e^{\frac{x}{y}}$ prove that $\frac{dy}{dx} = \frac{x-y}{x \log x}$

11. Diff. $\sin^{-1} \sqrt{\cos x}$ w.r.t x

12. Diff. $\frac{\sin^{-1} x}{\sqrt{1-x^2}}$ w.r.t. x

13. Diff. $\tan^{-1}\left(\frac{\cos x}{1+\sin x}\right)$ w.r.t.x

14. Diff. $\tan^{-1}\left(\frac{\sqrt{1+x^2}+1}{x}\right)$ w.r.t.x

15. Diff. $\tan^{-1}\left(\frac{x}{1+\sqrt{1-x^2}}\right)$ w.r.t.x

16. Diff. $\tan^{-1}\left(\frac{\sqrt{1+x^2}-\sqrt{1-x^2}}{\sqrt{1+x^2}+\sqrt{1-x^2}}\right)$ w.r.t. x

17. If $y = \tan^{-1}\left(\frac{5ax}{a^2-6x^2}\right)$ prove that $\frac{dy}{dx} = \frac{3a}{a^2+9x^2} + \frac{2a}{a^2+4x^2}$

18. Diff. $\sec^{-1}\left(\frac{4x-5}{4x+5}\right) + \sin^{-1}\left(\frac{4x+5}{4x-5}\right)$ w.r.t.x

19. If $y = \sec^{-1}\left(\frac{1+x^2}{1-x^2}\right) + \sin^{-1}\left(\frac{2x}{1+x^2}\right)$ prove $\frac{dy}{dx} = \frac{4}{1+x^2}$

20. Diff. $\sin^{-1}\left(x\sqrt{1-x}-\sqrt{x}\sqrt{1-x^2}\right)$ w.r.t.x

21. Diff. $\tan(\sin^{-1}x)$ w.r.t x

22. Diff. $\frac{\tan^{-1}x}{1+x^2}$ w.r.t. x

23. Diff. $\sec^{-1}\left(\frac{1}{2x^2-1}\right)$ w.r.t.x

24. Diff. $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$ w.r.t.x

25. Diff. $\cos^{-1}\left(\sqrt{\frac{1+x}{2}}\right)$ w.r.t.x

26. Diff. $\tan^{-1}\left(\frac{\sqrt{1+x^2}-\sqrt{1-x^2}}{\sqrt{1+x^2}+\sqrt{1-x^2}}\right)$ w.r.t. x

27. If $y = \tan^{-1}\frac{4x}{1+5x^2} + \tan^{-1}\frac{2+3x}{3-2x}$ find $\frac{dy}{dx}$

28. Diff. $\tan^{-1}\frac{4-5x}{4+5x} + \tan^{-1}\frac{4+5x}{4-5x}$ w.r.t.x

29. If $y = \sin^{-1}\frac{x}{\sqrt{1+x^2}} + \cos^{-1}\frac{1}{\sqrt{1+x^2}}$ prove $\frac{dy}{dx} = \frac{2}{1+x^2}$

30. Diff. $\sin^{-1}\left(x^2\sqrt{1-x^2} + x\sqrt{1-x^4}\right)$ w.r.t.x

31. Diff. $e^{\tan^{-1}x^2}$ w.r.t.x

32. Diff. $e^x \sin 4x$ w.r.t.x

33. Diff. $\log(x + \sqrt{x^2 + a^2})$ w.r.t.x

34. Diff. $\frac{e^{4x}}{\log 5x}$ w.r.t.x

35. Diff. $\log \sin \sqrt{x^2 + 1}$ w.r.t.x

36. Diff. $\log \tan\left(\frac{\pi}{4} + \frac{x}{2}\right)$ w.r.t.x

37. Find $\frac{dy}{dx}$, $xy + x e^{-y} + y e^x = x^2$

38.If $e^{x+y} = xy$ prove that $\frac{dy}{dx} = \frac{y(1-x)}{x(y-1)}$

39.Diff. $\log_{10} \sin x$ w.r.t.x

40.Find $\frac{dy}{dx}$ by first principle e^{5x} .