

TEST YOUR GRIP

CONTINUITY

1. The function $f(x) = [x]$ is discontinuous. At all points of the set of
2. The number of points of which the function $f(x) = \frac{1}{\log|x|}$ is discontinuous is...
3. An example of a function which is continuous everywhere and differentiable at all points except 0 is
4. Domain of continuity of the function $f(x) = |x-1|$
5. If f is continuous on its domain D , then $|f|$ is also continuous on D . (T/F)
6. The function $f(x) = \log x^2$ has only one point of discontinuity. (T/F).
7. If fg is continuous at $x=a$ then both f and g are separately continuous at $x=a$. (T/F)
8. An increasing function is always a continuous function. (T/F)
9. The function $f(x) = |x-1|$ is a continuous function. (T/F)
10. Examine for continuity, $f(x) = \begin{cases} \frac{2x^2-3x-2}{x-2}, & x \neq 2 \\ 3, & x = 2 \end{cases}$ at $x=2$
11. Examine for continuity, $f(x) = \begin{cases} \frac{|x-3|}{x-3}, & x \neq 3 \\ 3, & x = 3 \end{cases}$ at $x=3$
12. Examine for continuity $f(x) = |x| + |x-1|$ at $x=1$

13. Find the value of k so that f defined below is cont. at x=0

$$f(x) = \begin{cases} \frac{1 - \cos 4x}{5x^2}, & x \neq 0 \\ k, & x = 0 \end{cases}$$

14. Discuss the cont. f(x) =

$$\begin{cases} \frac{\sqrt{1+4x} - \sqrt{1-4x}}{\tan x}, & x \neq 0 \\ 4, & x = 0 \end{cases} \text{ at } x=0$$

15. If the function $f(x) = \begin{cases} 3ax + b & \text{if } x > 1 \\ 11 & \text{if } x = 1 \\ 5ax - 2b & \text{if } x < 1 \end{cases}$ is cont. at x=1, find a and b

16. For what value of k, $f(x) = \begin{cases} \frac{\sin 5x}{3x} & \text{if } x \neq 0 \\ k & \text{if } x = 0 \end{cases}$ cont. at x=0

17. Discuss cont. $f(x) = \begin{cases} (x-2)\sin \frac{1}{x-2} & \text{if } x \neq 2 \\ 0 & \text{if } x = 2 \end{cases}$ at x=2

18. Discuss the cont. $f(x) = \begin{cases} \frac{e^{1/x} - 1}{e^{1/x} + 1} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$ at x=0

19. Find the value of k for which the function

$$f(x) = \begin{cases} \frac{k \cos x}{\pi - 2x}, & x < \frac{\pi}{2} \\ 3, & x = \frac{\pi}{2} \\ \frac{3 \tan 2x}{2x - \pi}, & x > \frac{\pi}{2} \end{cases} \text{ at } x = \frac{\pi}{2}$$

20. Discuss the cont. $f(x) = \begin{cases} \frac{x-3}{\sqrt{x^2-9}} & , x \neq 3 \\ 0 & , x = 3 \end{cases}$ at $x=3$

21. Show that $f(x) = x - [x]$ is discontinuous at all integral points.

22. Show that $f(x) = |\cos x|$ is a continuous function.

23. Show that $f(x) = \sin x^2$ is continuous.

24. Find a and b such that

$$f(x) = \begin{cases} 3ax + 2b + 1 & , x \leq 1 \\ 5bx - a + 7 & , 1 < x < 4 \\ 2ax - bx^2 + 3 & , x \geq 4 \end{cases} \text{ cont. at } x=1 \text{ and } x=4$$