

SELF ASSESSMENT TEST -4

CLASS B.A, B.SC-1

SUCCESSIVE DIFFERENTIATION

1. Prove that $\frac{d^n}{dx^n} \left(\frac{\log x}{x} \right) = \frac{(-1)^n n!}{x^{n+1}} \left[\log x - 1 - \frac{1}{2} - \frac{1}{3} \dots \dots \frac{1}{n} \right]$.

2. Find the nth derivative if $y = \frac{2x+1}{(x-2)(x-3)}$.

3. Find the nth derivative of $\sin^2 x \cos^3 x$

4. Find the nth derivative of $\frac{1}{x^2+a^2}$ if $\theta = \cot^{-1} \frac{x}{a}$.

5. State and prove Leibnitz's thm.

6. Find the value of the nth derivative of $e^{m \cos^{-1} x}$ at $x=0$.

7. If $f(x) = \tan x$, prove that

$$f^n(0) - C(n,2) f^{n-2}(0) + C(n,4) f^{n-4}(0) - \dots = \sin \frac{n\pi}{2}$$

8. If $y = \sin(m \sin^{-1} x)$ prove that $(1-x^2)y_{n+2} - (2n+1)x y_{n+1} - (n^2 - m^2)y_n = 0$

deduce that $y_n(0) = \begin{cases} 0 & n \text{ even} \\ m(1^2 - m^2)(3^2 - m^2) \dots \dots \dots ((n-2)^2 - m^2) & n \text{ odd} \end{cases}$.

9. Use Leibnitz's thm find the nth derivative of $e^x \log x$