

**SELF ASSESSMENT TEST -3****CLASS B.A/B.SC-1**

## TRANSFORMATION OF EQUATIONS

1. Remove the fractional coeff.so that the leading coeff remains

unity of eqn  $x^3 - \frac{7}{3}x^2 + \frac{11}{36}x - \frac{25}{72} = 0$

2. Solve  $3x^3 - 22x^2 + 48x - 32 = 0$  , its roots being in H.P.

3. Increase the roots of the eqn  $2x^3 + x^2 - 13x + 6 = 0$  by 3 and hence solve the eqn.

4. Show that the same transformation removes second and fourth terms of the eqn.  $x^4 + 20x^3 + 143x^2 + 430x + 462 = 0$  . obtain the transformed eqn and solve

5. Find the eqn whose roots are the squares of the roots of the eqn

$x^3 - 5x^2 + 17x - 13 = 0$  Hence find the nature of the roots of given eqn

- 6.If  $\alpha, \beta, \gamma$  are the roots of  $x^3 + x + 2 = 0$  , then form an eqn whose roots are  $\beta\gamma + \frac{1}{\alpha}, \alpha\beta + \frac{1}{\gamma}, \alpha\gamma + \frac{1}{\beta}$  .

7. If  $\alpha, \beta, \gamma$  are the roots of the roots of the eqn  $x^3 + 2x^2 + x - 1 = 0$  , form an eqn whose roots are  $\frac{1}{\beta^3} + \frac{1}{\gamma^3} - \frac{1}{\alpha^3}, \frac{1}{\alpha^3} + \frac{1}{\beta^3} - \frac{1}{\gamma^3}, \frac{1}{\gamma^3} + \frac{1}{\alpha^3} - \frac{1}{\beta^3}$  .

- 8.Find the eqn of the squared differences of the roots of the cubic

$x^3 + 6x^2 + 7x + 2 = 0$  .

- 9.Form an equation whose roots are the roots of the eqn.

$2x^5 - 7x^4 + 8x^3 + x^2 - 2x + 4 = 0$  With their sign changed.

10. Solve  $6x^3 - 11x^2 + 6x - 1 = 0$ , given that its roots are in H.P.

11. solve  $15x^4 - 8x^3 - 14x^2 + 8x - 1 = 0$ , given that its roots are in H.P.

12. Transform the eqn  $x^4 - 4x^3 - 18x^2 + 5x + 8 = 0$  into one in which the third term is missing

13. Find the condition that the second and third terms of the cubic

$$a_0x^3 + 3a_1x^2 + 3a_2x + a_3 = 0$$

are removed by single transformation.

Hence solve  $x^3 - 12x^2 + 48x - 72 = 0$

14. Find the eqn whose roots are cubes of the roots of eqn

$$x^4 - 2x^3 - x^2 + 2x + 1 = 0$$

15. If  $\alpha, \beta, \gamma$  are the roots of the eqn  $x^3 + 2x + 1 = 0$ , then form eqn whose

roots are  $\frac{\beta}{\alpha} + \frac{\alpha}{\beta}, \frac{\beta}{\gamma} + \frac{\gamma}{\beta}, \frac{\gamma}{\alpha} + \frac{\alpha}{\gamma}$ .

16. If  $\alpha, \beta, \gamma$  are the roots of the eqn  $x^3 + px^2 + qx + r = 0$ , then form eqn

whose roots are  $\beta\gamma - \alpha^2, \gamma\alpha - \beta^2, \alpha\beta - \gamma^2$ .

17. Find an eqn whose roots are the squares of the difference of the roots of  $x^3 - 3x + 1 = 0$ .

18. Find the eqn whose roots are the squares of the difference of the roots of  $x^3 + 6x^2 + 2 = 0$

19. Find the eqn of the squared diff. of the roots of the cubic

$$x^3 + 6x^2 + 7x + 2 = 0$$

20.If  $\alpha, \beta, \gamma$  are the roots of  $2x^3 + x^2 + x + 1 = 0$  , form an eqn whose roots are  $\frac{1}{\alpha^2} + \frac{1}{\beta^2} - \frac{1}{\gamma^2}, \frac{1}{\beta^2} + \frac{1}{\gamma^2} - \frac{1}{\alpha^2}, \frac{1}{\gamma^2} + \frac{1}{\alpha^2} - \frac{1}{\beta^2}$  .

21.If  $\alpha, \beta, \gamma$  are the roots of  $x^3 + x + 2 = 0$  then form an eqn whose roots are  $\beta^2 + \beta\gamma + \gamma^2, \alpha^2 + \alpha\beta + \beta^2, \gamma^2 + \gamma\alpha + \alpha^2$  .

22.Find the eqn whose roots are the cubes of the roots of the eqn  $x^4 - x^3 + 2x^2 + 3x + 1 = 0$

23.Find the eqn whose roots are the squares of the roots of the eqn  $x^3 - x^2 - 2x + 2 = 0$  .

24.Show that the same transformation removes both second and fourth terms of the eqn  $x^4 + 16x^3 + 83x^2 + 152x + 84 = 0$  .

25.Transform the eqn  $2x^3 - 15x^2 + 24x - 7 = 0$  in which the third term is missing

26.Use the multiplier to remove the fractional coeff. of the eqn

$$x^3 - \frac{3}{2}x^2 - \frac{1}{16}x + \frac{1}{9} = 0 .$$

