

TOPICS COVERED

FUNCTIONS

1. The domain of the function $f(x) = \frac{1}{\sqrt{x^2 - 3x + 2}}$ is
- (1) $(-\infty, 1)$ (2) $(-\infty, 1) \cap (2, \infty)$
 (3) $(-\infty, 1) \cup (2, \infty)$ (4) $(2, \infty)$
2. The domain of the function $f(x) = \sqrt{x - \sqrt{1 - x^2}}$ is
- (1) $\left[-1, -\frac{1}{\sqrt{2}}\right] \cup \left[\frac{1}{\sqrt{2}}, 1\right]$ (2) $[-1, 1]$
 (3) $\left(-\infty, -\frac{1}{2}\right] \cup \left[\frac{1}{\sqrt{2}}, +\infty\right)$ (4) $\left[\frac{1}{\sqrt{2}}, 1\right]$
3. The domain of the function $f(x) = \sqrt{2 - 2x - x^2}$ is
- (1) $[-\sqrt{3}, \sqrt{3}]$
 (2) $[-1 - \sqrt{3}, -1 + \sqrt{3}]$
 (3) $[-2, 2]$
 (4) $[-2, -\sqrt{3}, -2 + \sqrt{3}]$
4. The domain of the function $f(x) = \frac{1}{\sqrt{x^{12} - x^9 + x^4 - x + 1}}$ is
- (1) $(-\infty, -1)$ (2) $(1, \infty)$
 (3) $(-1, 1)$ (4) $(-\infty, \infty)$
5. The domain of the function $f(x) = \sqrt{\frac{(x+1)(x-3)}{(x-2)}}$ is given by
- (1) $[-1, 2) \cup [3, \infty)$ (2) $(-1, 2) \cup [3, \infty)$
 (3) $[-1, 2] \cup [3, \infty)$ (4) none of these
6. The domain of the function $f(x) = \sqrt{x-1} + \sqrt{5-x}$ is
- (1) $[1, \infty)$ (2) $(-\infty, 5)$
 (3) $(1, 5)$ (4) $[1, 5]$
7. The domain of the function $f(x) = \sqrt{1 - \sqrt{1 - \sqrt{1 - x^2}}}$ is
- (1) $(-\infty, 1)$ (2) $(-1, \infty)$
 (3) $[0, 1]$ (4) $[-1, 1]$
8. The domain of the function $f(x) = \sqrt{\frac{x+3}{(2-x)(x-5)}}$ is
- (1) $(-\infty, -3] \cup (2, 5)$ (2) $(-\infty, 3) \cup (2, 5)$
 (3) $(-\infty, 3) \cup [2, 5]$ (4) none of these
9. The domain of the function $f(x) = \frac{1}{\sqrt{|x| - x}}$ is
- (1) $(0, \infty)$ (2) $(-\infty, 0)$
 (3) $(-\infty, \infty)$ (4) none of these
10. The domain of definition of $f(x) = \sqrt{\frac{1-|x|}{2-|x|}}$ is
- (1) $(-\infty, \infty) - [-1, 1]$
 (2) $(-\infty, \infty) - [-2, 2]$

(3) $[-1, 1] \cup (-\infty, -2) \cup (2, \infty)$

(4) none of these

11. The domain of definition of the

function $y = \sqrt{\log_{10} \left(\frac{5x - x^2}{4} \right)}$ is

(1) $[1, 4]$ (2) $(1, 4)$

(3) $[1, 4)$ (4) $(1, 4]$

12. The domain of definition of the function

$y = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$ is

(1) $[-2, 1]$ (2) $[-2, 1[$

(3) $[-2, 0[\cup]0, 1[$ (4) none of these

13. The domain of the function

$f(x) = \log_{10} \frac{x-5}{x^2-10x+24} - \sqrt[3]{x+5}$ is

(1) $(4, 5)$ (2) $(6, \infty)$

(3) $(4, 5) \cup (6, \infty)$ (4) $(4, 5] \cup (6, \infty)$

14. The domain of the function

$f(x) = \sqrt{\log_{10} \frac{3-x}{x}}$ is

(1) $\left(0, \frac{3}{2}\right)$ (2) $(0, 3)$

(3) $\left(-\infty, \frac{3}{2}\right]$ (4) $\left(0, \frac{3}{2}\right]$

15. The domain of the function $f(x) = \log_{10} |4 - x^2 - |$ is

(1) $(-\infty, \infty) - (2, 2)$ (2) $(0, \infty)$

(3) $(-\infty, 0)$ (4) none of these

16. The domain of the function

$f(x) = \log_2 \log_3 \log_4 x$ is

(1) $[4, \infty)$ (2) $(4, \infty)$

(3) $(-\infty, 4)$ (4) none of these

17. The domain of the function

$f(x) = \frac{1}{\log_3(x-2)} + \sqrt{5-x}$ is

(1) $[2, 3] - \{3\}$ (2) $(2, 5] - \{3\}$

(3) $[2, 5] - \{3\}$ (4) $(2, 5) - \{3\}$

18. The domain of the function

$f(x) = \log_{10}(\sqrt{x-4} + \sqrt{6-x})$ is

(1) $(4, 6)$ (2) $[4, 6]$

(3) $[4, 6)$ (4) none of these

19. The domain of the function

$f(x) = \log_{10} [1 - \log_{10}(x^2 - 5x + 16)]$

(1) $(2, 3)$ (2) $[2, 3]$

(3) $(2, 3]$ (4) $[2, 3)$

20. The domain of the function

$f(x) = \log_{1/2} \left(x - \frac{1}{2}\right) + \log_2 \sqrt{4x^2 - 4x + 5}$

is

(1) $\left[\frac{1}{2}, \infty\right)$ (2) $\left(\frac{1}{2}, \infty\right)$

(3) $(-\infty, \infty)$ (4) none of these

21. The domain of the function

$f(x) = \log_{10} \sin(x-3) + \sqrt{16-x^2}$ is

(1) $(3, 4)$ (2) $(-4, 4)$

(3) $(3, \pi+3)$ (4) none of these

22. The domain of the function $f(x) = \log_x \cos x$ is

(1) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right) - \{1\}$ (2) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right] - \{1\}$

(3) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ (4) none of these

23. The domain of the function

$f(x) = \frac{1}{\sqrt{|\sin x| + \sin x}}$ is

(1) $(-2n\pi, 2n\pi)$

- (2) $(2n\pi, (2n+1)\pi)$
- (3) $\left((4n-1)\frac{\pi}{2}, (4n+1)\frac{\pi}{2} \right)$
- (4) none of these
24. The domain of the function $f(x) = \sin^{-1} \left\{ \log_2 \left(\frac{1}{2} x^2 \right) \right\}$ is
- (1) $[-2, -1] \cup [1, 2]$ (2) $(-2, -1) \cup [1, 2]$
- (3) $[-2, -1] \cup [1, 2]$ (4) $(-2, -1) \cup (1, 2)$
25. The domain of the function $f(x) = \frac{\sqrt{9-x^2}}{\sin^{-1}(3-x)}$ is
- (1) $(2, 3)$ (2) $[2, 3]$
- (3) $(2, 3]$ (4) none of these
26. The domain of the function $f(x) = \sqrt{3-x} + \cos^{-1} \left(\frac{3-2x}{5} \right)$
- (1) $[-1, 3]$ (2) $(-1, 3]$
- (3) $[-1, 3)$ (4) none of these
27. The domain of the function $f(x) = \sin^{-1} \left(\frac{1+x^3}{2x^{3/2}} \right) + \sqrt{\sin(\sin x) + \log_{(3(x+1))} (x^2+1)}$ where $\{ \}$ represents fractional part function, is
- (1) $\{1\}$ (2) $\mathbb{R} - \{1, -1\}$
- (3) $x > 3, x \notin 1$ (4) none of these
28. The domain of the function $f(x) = \frac{1}{1-x} + 2^{\sin^{-1} x} + \frac{1}{\sqrt{x-2}}$ is
- (1) $(-\infty, \infty) - \{1\}$ (2) $(2, \infty)$
- (3) $[-1, 1)$ (4) ϕ
29. The domain of the function $f(x) = \cos^{-1} \left(\frac{2-|x|}{4} \right) + [\log(3-x)]^{-1}$
- (1) $[-6, 3) - \{2\}$ (2) $[-6, 2) \cup (2, 3]$
- (3) $[-6, 3]$ (4) $[-6, 3)$
30. The domain of the function $f(x) = \sin^{-1} \left(\frac{x-3}{2} \right) - \log_{10}(4-x)$ is
- (1) $(1, 4)$ (2) $[1, 4]$
- (3) $[1, 4)$ (4) $(1, 4]$
31. The domain of the function $f(x) = \cos^{-1} \left(\frac{3}{4+2\sin x} \right)$ is
- (1) $\left[-\frac{\pi}{6} + 2n\pi, \frac{\pi}{6} + 2n\pi \right]$
- (2) $\left(-\frac{\pi}{6} + 2n\pi, \frac{\pi}{6} + 2n\pi \right)$
- (3) $\left(-\frac{\pi}{6} + 2n\pi, \frac{\pi}{6} + 2n\pi \right]$
- (4) $\left[-\frac{\pi}{6} + 2n\pi, \frac{\pi}{6} + 2n\pi \right)$
32. The domain of the function $f(x) = \sin^{-1} \left(\frac{4}{3+2\cos x} \right)$ is
- (1) $2n\pi - \frac{\pi}{6} \leq x \leq 2n\pi + \frac{\pi}{6}, n \in I$
- (2) $0 \leq x \leq 2n\pi + \frac{\pi}{6}, n \in I$
- (3) $2n\pi - \frac{\pi}{6} < x < 2n\pi + \frac{\pi}{6}, n \in I$
- (4) $2n\pi - \frac{\pi}{6} \leq x \leq 0, n \in I$
33. The domain of the function $f(x) = \tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2+x+1}$ is
- (1) $[-1, 0]$ (2) $\{-1, 0\}$
- (3) $(-\infty, -1] \cup [0, \infty)$ (4) $(-\infty, \infty)$

34. The domain of the function $f(x) = \sqrt[3]{1-3x} + 3 \cos^{-1}\left(\frac{2x-1}{3}\right) + e^{3 \tan x}$ is
- (1) $[-1, 2]$ (2) $(-1, 2)$
 (3) $(-\infty, \infty)$ (4) none of these
35. Let $f(x) = (-1)^{[x]}$ (where $[.]$ denotes the greatest integer function), then
- (1) Range of f is $\{-1, 1\}$
 (2) f is an even function
 (3) f is an odd function
 (4) $\lim_{x \rightarrow n} f(x)$ exists, for every integer n
36. The domain of the function $f(x) = \frac{1}{\sqrt{[x]^2 - [x] - 6}}$ is
- (1) $(-\infty, -2) \cup [4, \infty)$ (2) $(-\infty, -2] \cup [4, \infty)$
 (3) $(-\infty, -2) \cup (4, \infty)$ (4) none of these
37. The domain of the function $f(x) = \sqrt{x^2 - [x]^2}$, where $[x]$ denotes the greatest integer less than or equal to x , is
- (1) $(0, \infty)$ (2) $(-\infty, 0)$
 (3) $(-\infty, \infty)$ (4) none of these
38. Which of the following is a function ($[.]$ denotes the greatest integer function, $\{.\}$ denotes the fractional part function)?
- (1) $\frac{1}{\log[1-|x|]}$ (2) $\frac{x!}{\{x\}}$
 (3) $x!\{x\}, x \in N$ (4) $\frac{\log(x-1)}{\sqrt{1-x^2}}$
39. Range of the function f defined by $f(x) = \left[\frac{1}{\sin\{x\}} \right]$ (where $[.]$ and $\{.\}$ respectively denote the greatest integer and the fractional part functions) is
- (1) I, the set of integers (2) N, the set of natural numbers
 (3) W, the set of whole numbers (4) $\{2, 3, 4, \dots\}$
40. The range of the function $y = \frac{x}{1+x^2}$ is
- (1) $\left[0, \frac{1}{2}\right]$ (2) $\left[-\frac{1}{2}, \frac{1}{2}\right]$
 (3) $\left[-\frac{1}{2}, 0\right]$ (4) none of these
41. The range of the function $y = \frac{x^2}{1+x^2}$ is
- (1) $[0, 1[$ (2) $[0, 1]$
 (3) $]0, 1[$ (4) none of these
42. The range of the function $y = \frac{1}{2 - \sin 3x}$ is
- (1) $\left(\frac{1}{3}, 1\right)$ (2) $\left[\frac{1}{3}, 1\right)$
 (3) $\left[\frac{1}{3}, 1\right]$ (4) none of these
43. The range of the function $f(x) = \log_e(3x^2 - 4x + 5)$ is
- (1) $\left(-\infty, \log_e \frac{11}{3}\right]$ (2) $\left[\log_e \frac{11}{3}, \infty\right)$
 (3) $\left[-\log_e \frac{11}{3}, \log_e \frac{11}{3}\right]$ (4) none of these
44. The range of the function $y = 3 \sin \sqrt{\frac{\pi^2}{16} - x^2}$ is
- (1) $\left[0, \frac{3}{\sqrt{2}}\right]$ (2) $\left[-\frac{3}{\sqrt{2}}, \frac{3}{\sqrt{2}}\right]$
 (3) $\left[-\frac{3}{\sqrt{2}}, 0\right]$ (4) none of these
45. The range of the function

$$f(x) = \sqrt{3x^2 - 4x + 5} \text{ is}$$

(1) $\left[-\infty, \sqrt{\frac{11}{3}}\right]$ (2) $\left(-\infty, \sqrt{\frac{11}{3}}\right)$

(3) $\left[\sqrt{\frac{11}{3}}, \infty\right)$ (4) $\left(\sqrt{\frac{11}{3}}, \infty\right)$

46. The range of the function $y = \sin^{-1}\left(\frac{x^2}{1+x^2}\right)$ is

(1) $\left(0, \frac{\pi}{2}\right)$ (2) $\left[0, \frac{\pi}{2}\right)$

(3) $\left[0, \frac{\pi}{2}\right]$ (4) none of these

47. If $A = \left\{x : \frac{\pi}{6} \leq x \leq \frac{\pi}{3}\right\}$ and

$f(x) = \cos x - x(1+x)$, then $f(A)$ is equal to

(1) $\left[\frac{1}{2} - \frac{\pi}{2} - \frac{\pi^2}{9}, \frac{\sqrt{3}}{2} - \frac{\pi}{6} - \frac{\pi^2}{36}\right]$

(2) $\left[\frac{1}{2} + \frac{\pi}{3} - \frac{\pi^2}{9}, \frac{\sqrt{3}}{2} + \frac{\pi}{6} - \frac{\pi^2}{36}\right]$

(3) $\left(\frac{1}{2} - \frac{\pi}{3} - \frac{\pi^2}{9}, \frac{\sqrt{3}}{2} - \frac{\pi}{6} - \frac{\pi^2}{36}\right)$

(4) none of these

48. Range of values of

$$f(x) = 1 + \sin x + \sin^3 x + \sin^5 x \dots,$$

$$x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \text{ is}$$

(1) $(0, 1)$ (2) $(-\infty, \infty)$

(3) $(-2, 2)$ (4) none of these

49. The range of the function

$$f(x) = \tan \sqrt{\frac{\pi^2}{9} - x^2} \text{ is}$$

(1) $[0, \sqrt{3}]$

(2) $(0, \sqrt{3})$

(3) $[0, \sqrt{3})$

(4) $(0, \sqrt{3}]$

50. The function $f(x) = \log(x + \sqrt{x^2 + 1})$ is

(1) an even function

(2) an odd function

(3) a periodic function

(4) neither an even nor an odd function

51. A function whose graph is symmetrical about the y -axis is given by

(1) $f(x) = \sin \left[\log(x + \sqrt{x^2 + 1}) \right]$

(2) $f(x) = \frac{\sec^4 x + \csc^4 x}{x^3 + x^4 \cot x}$

(3) $f(x+y) = f(x) + f(y), \forall x, y \in R$

(4) none of the above

52. If f is an even function and g is an odd function, then the function fog is

(1) an even function

(2) an odd function

(3) neither even nor odd

(4) a periodic function

53. If f is an odd function and g is an even function, then the function fog is

(1) an even function

(2) an odd function

(3) neither even nor odd

(4) a periodic function

54. Let f and g be two odd functions, then the function fog is

(1) an even function

(2) an odd function

(3) neither even nor odd

(4) a periodic function

55. The functions

$$f(x) = \log(x-1) - \log(x-2) \quad \text{and}$$

$$g(x) = \log\left(\frac{x-1}{x-2}\right) \text{ are identical when } x \text{ lies}$$

in the interval

- (1) $[1, 2]$ (2) $[2, \infty]$ (1) 2π (2) $\frac{2\pi}{3}$
 (3) $(2, \infty)$ (4) $(-\infty, \infty)$ (3) $\frac{\pi}{3}$ (4) none of these
56. The period of the $f(x) = \frac{|\sin x| - |\cos x|}{|\sin x + \cos x|}$, is
 (1) $\frac{\pi}{2}$ (2) 2π (3) $\frac{\pi}{3}$ (4) none of these
57. The period of the function $f(x) = \sin^4 x + \cos^4 x$ is
 (1) π (2) $\frac{\pi}{2}$ (3) $\frac{\pi}{2}$ (4) none of these
58. Which of the following function has period π ?
 (1) $2 \cos\left(\frac{2\pi x}{3}\right) + 3 \sin\left(\frac{\pi x}{3}\right)$
 (2) $|\tan x| + \cos 2x$
 (3) $4 \cos\left(2\pi x + \frac{\pi}{2}\right) + 2 \sin\left(\pi x + \frac{\pi}{4}\right)$
 (4) none of the above
59. The period of the function $f(x) = x[x]$ is
 (1) 1 (2) 2
 (3) non periodic (4) none of these
60. period of the function $\log(\sin^{-1}(x - [x]))$ ($[\cdot]$ denotes the greatest integer function) is
 (1) 1 (2) 2π
 (3) $\frac{\pi}{2}$ (4) none of these
61. If $f: R \rightarrow R$ is a function satisfying the property $f(2x+3) + f(2x+7) = 2$,
 $\forall x \in R$, then the period of $f(x)$ is
 (1) 2 (2) 4
 (3) 8 (4) 12
62. The period of the function $f(x) = 7 \cos(3x+5)$ is
 (1) 2π (2) $\frac{2\pi}{3}$
 (3) $\frac{\pi}{3}$ (4) none of these
63. The period of the function $f(x) = a \sin kx + b \cos kx$ is
 (1) $\frac{2\pi}{k}$ (2) $\frac{2\pi}{|k|}$
 (3) $\frac{\pi}{|k|}$ (4) none of these
64. The period of the function $f(x) = \cos x^2$ is
 (1) 2π (2) π
 (3) $\frac{\pi}{2}$ (4) none of these
65. The period of the function $f(x) = |\sin 4x| + |\cos 4x|$ is
 (1) $\frac{\pi}{2}$ (2) $\frac{\pi}{8}$
 (3) $\frac{\pi}{4}$ (4) none of these
66. If $f(x) = \sqrt{3|x| - x - 2}$ and $g(x) = \sin x$, then domain of definition of $\text{fog}(x)$ is
 (1) $\left\{2n\pi + \frac{\pi}{2}\right\}_{n \in \mathbb{Z}}$
 (2) $\bigcup_{n \in \mathbb{Z}} \left(2n\pi + \frac{7\pi}{6}, 2n\pi + \frac{11\pi}{6}\right)$
 (3) $\left\{2n\pi + \frac{7\pi}{6}\right\}_{n \in \mathbb{Z}}$
 (4) $\left(2n\pi + \frac{7\pi}{6}, 2n\pi + \frac{11\pi}{6}\right) \bigcup_{n, m \in \mathbb{Z}} \left(2m\pi + \frac{\pi}{2}\right)$
67. Let $f(x)$ be a function defined on $[0, 1]$ such that $f(x) = \begin{cases} x & x \in Q \\ 1-x & x \notin Q \end{cases}$ then for all

$x \in [0, 1]$, $f \circ f(x)$ is

- (1) a constant (2) $1+x$
 (3) x (4) none of these

68. If $f(x) = 1-x$, $x \in [-3, 3]$, then the domain of $f[f(x)]$ is

- (1) $[-2, 3]$ (2) $(-2, 3)$
 (3) $[-2, 3)$ (4) $(-2, 3]$

69. If $f(x) = \frac{1-x}{1+x}$; $x \neq 0$, then

- $f[f(x)] + f\left[f\left(\frac{1}{x}\right)\right]$
 (1) < 2 (2) ≥ 2
 (3) $= 2$ (4) non of these

70. $f(x) = \begin{cases} |x|, & x \leq 1 \\ 2-x, & x > 1 \end{cases}$, then $f[f(x)]$ is equal to

(1) $\begin{cases} 2-|x|, & x < -1 \\ |x|, & -1 \leq x \leq 1 \\ |2-x|, & x > 1 \end{cases}$

(2) $\begin{cases} |x|, & x < -1 \\ 2-|x|, & -1 \leq x \leq 1 \\ |2-x|, & x > 1 \end{cases}$

(3) $\begin{cases} |2-x|, & x < -1 \\ |x|, & -1 \leq x \leq 1 \\ 2-|x|, & x > 1 \end{cases}$

(4) none of these

71. The function $f : (-\infty, -1] \rightarrow (0, e^5)$ defined

by $f(x) = e^{x^3-3x+2}$, is

- (1) many one and onto (2) many one and into
 (3) one-one and onto (4) one-one and into

72. A function f from the set of natural numbers to integers defined by

$$f(n) = \begin{cases} \frac{n-1}{2}, & \text{where } n \text{ is odd} \\ -\frac{n}{2}, & \text{where } n \text{ is even} \end{cases}$$

- (1) one-one but not onto
 (2) onto but not one-one
 (3) one-one and onto both
 (4) neither one-one nor onto

73. The function $f : \mathbb{R} \rightarrow \mathbb{R}$, defined by $f(x) = [x]$, $\forall x \in \mathbb{R}$, is

- (1) one-one (2) onto
 (3) both one-one and onto
 (4) neither one-one nor onto

74. Let $f : \mathbb{R} \rightarrow \mathbb{R}$, be a function defined by $f(x) = \sin(2x-3)$, then f is

- (1) injective (2) surjective
 (3) bijective (4) none of these

75. Which of the following functions from \mathbb{I} to itself are bijections ?

- (1) $f(x) = x+3$ (2) $f(x) = x^5$
 (3) $f(x) = 3x+2$ (4) $f(x) = x^2+x$

76. Which of the following functions is (are) injective map(s) ?

- (1) $f(x) = x^2+2, x \in (-\infty, \infty)$
 (2) $f(x) = |x+2|, x \in [-2, \infty)$
 (3) $f(x) = (x-4)(x-5), x \in (-\infty, \infty)$
 (4) $f(x) = \frac{4x^2+3x-5}{4+3x-5x^2}, x \in (-\infty, \infty)$

77. Let $A = \{x \in \mathbb{R} \mid -1 \leq x \leq 1\} = B$. then the mapping $f : A \rightarrow B$ is given by $f(x) = x|x|$, is

- (1) injective but not surjective
 (2) surjective but not injective
 (3) bijective (4) none of these

78. If the function $f : (-\infty, \infty) \rightarrow B$ defined by

$f(x) = -x^2 + 6x - 8$ is bijective, then B is equal to

- (1) $[1, \infty)$ (2) $(-\infty, 1]$
 (3) $(-\infty, \infty)$ (4) none of these

79. Let $f: R \rightarrow R$ be defined by

$$f(x) = \frac{x-a}{x-b}, \text{ where } a \neq b. \text{ then } f \text{ is}$$

- (1) injective but not surjective
 (2) surjective but not injective
 (3) bijective (4) none of the above

80. The number of bijective functions from a set of itself when A contains 106 elements, is

- (1) 106 (2) $(106)^2$
 (3) $(106)!$ (4) 2^{106}

81. The number of bijective functions from a set

$$A = \{1, 2, \dots, n\}, n \geq 2 \text{ onto } B = \{a, b\} \text{ is}$$

- (1) ${}^n P_2$ (2) $2^2 - 2$
 (3) $2^2 - 1$ (4) none of these

82. Set A has 3 elements and set B has 4 elements. The number of injections that can be defined from A to B is

- (1) 144 (2) 12
 (3) 24 (4) 64

83. Let $f: (4, 6) \rightarrow (6, 8)$ be a function defined

$$\text{by } f(x) = x + \left[\frac{x}{2} \right] \text{ (where } [.] \text{ denotes the}$$

greatest integer function), then $f^{-1}(x)$ is equal to

- (1) $x - \left[\frac{x}{2} \right]$ (2) $-x - 2$

- (3) $x - 2$ (4) $x + \left[\frac{x}{2} \right]$

84. The value of the parameter α , for which the function $f(x) = 1 + \alpha x, \alpha \neq 0$ is the inverse of

itself, is

- (1) -2 (2) -1
 (3) 1 (4) 2

85. The inverse of the function $f(x) = \frac{a^x - a^{-x}}{a^x + a^{-x}}$ is

(1) $\frac{1}{2} \log_a \left(\frac{1-x}{1+x} \right)$ (2) $\frac{1}{2} \log_a \left(\frac{1+x}{1-x} \right)$

(3) $\log_a \left(\frac{1+x}{1-x} \right)$ (4) none of these

86. If the $f: [1, \infty) \rightarrow [1, \infty)$ function is defined by

$$f(x) = 2^{x(x-1)}, \text{ then } f^{-1}(x) \text{ is}$$

(1) $\left(\frac{1}{2} \right)^{x(x-1)}$
 (2) $\left(\frac{1}{2} \right) \left[1 + \sqrt{1 + 4 \log_2 x} \right]$

(3) $\left(\frac{1}{2} \right) \left[1 - \sqrt{1 + 4 \log_2 x} \right]$

(4) not defined

87. The inverse of the function

$$y = \left[1 - (x-3)^4 \right]^{1/7} \text{ is}$$

(1) $3 + (1-x^7)^{1/4}$ (2) $3 - (1-x^7)^{1/4}$

(3) $3 - (1+x^7)^{1/4}$ (4) none of these

88. If $f(n+1) = \frac{2f(n)+1}{2}, n = 1, 2, \dots$ and

$$f(1) = 2, \text{ then } f(101) \text{ equals}$$

- (1) 52 (2) 49
 (3) 48 (4) 51

89. The number of solutions of the equation

$$a^{f(x)} + g(x) = 0, a > 0, g(x) \neq 0 \text{ and has}$$

minimum value of $\frac{1}{2}$ is

- (1) one (2) two
 (3) zero (4) infinitely many

90. If $f: R \rightarrow R, g: R \rightarrow R$ be two given functions, then

$$f(x) = 2 \min\{|f(x) - g(x)|, 0\} \text{ equals}$$

(1) $f(x) + g(x) - |g(x) - f(x)|$

(2) $f(x) + g(x) + |g(x) - f(x)|$

(3) $f(x) - g(x) + |g(x) - f(x)|$

(4) $f(x) - g(x) - |g(x) - f(x)|$

91. If $f: R \rightarrow R$ satisfies

$$f(x+y) = f(x) + f(y), \text{ for all } x, y \in R$$

and $f(1) = 7$, then $\sum_{r=1}^n f(r)$ is

(1) $\frac{7n}{2}$

(2) $\frac{7(n+1)}{2}$

(3) $7n(n+1)$

(4) $\frac{7n(n+1)}{2}$

Goyal's Math

ADDITIONAL SOLVED EXAMPLES

1. If $[x]^2 - 5[x] + 6 = 6$, where $[.]$ denote the greatest integer function, then
 (1) $x \in [3, 4)$ (2) $x \in [2, 3)$
 (3) $x \in \{2, 3\}$ (4) $x \in [2, 4)$
2. If $\left[\log \left(\frac{x}{[x]} \right) \right] \geq 0$, where $[.]$ denote the greatest integer function, then
 (1) $x \in (-\infty, \infty) \sim [0, 1)$ (2) $(-\infty, 0)$
 (3) $(1, \infty)$ (4) none of these
3. Total number of positive real values of x satisfying $2[x] = x + \{x\}$, where $[.]$ and $\{.\}$ denote the greatest integer function and fractional part respectively, is equal to
 (1) 2 (2) 1
 (3) 0 (4) 3
4. Total number of solutions of $[x]^2 = x + 2\{x\}$, where $[.]$ and $\{.\}$ denotes the greatest integer function and fractional part respectively, is equal to
 (1) 2 (2) 4
 (3) 6 (4) none of these
5. Domain of $f(x) = \sqrt{\frac{x-1}{x-2\{x\}}}$, where $\{.\}$ denotes the fractional part of x , is
 (1) $(-\infty, 0) \cup (0, 2]$
 (2) $[1, 2)$
 (3) $(-\infty, \infty) \sim [0, 2)$
 (4) $(-\infty, 0) \cup (0, 1) \cup [2, 8)$
6. Domain of $f(x) = \sin^{-1} \left(\frac{[x]}{\{x\}} \right)$, where $[.]$ and $\{.\}$ denote the greatest integer function and fractional part respectively, is
 (1) $(0, 1)$ (2) $(-1, 1) \sim \{0\}$
 (3) $(-2, 2) \sim \{-1, 0, 1\}$ (4) none of these
7. Domain of $f(x) = \sqrt{2\{x\}^2 - 3\{x\} + 1}$, where $\{.\}$ denotes the fractional part, in $[-1, 1]$, is
 (1) $[-1, 1] \sim \left(\frac{1}{2}, 1\right)$
 (2) $\left[-1, -\frac{1}{2}\right] \cup \left[0, \frac{1}{2}\right] \cup \{1\}$
 (3) $\left[-1, \frac{1}{2}\right]$ (4) $\left[-\frac{1}{2}, 1\right]$
8. Domain of $f(x) = \sqrt{\cos(\sin x)} + \sqrt{\log_x \{x\}}$; where $\{.\}$ denotes the fractional part, is
 (1) $[1, \pi)$ (2) $(0, 2\pi) \sim [1, \pi)$
 (3) $\left(0, \frac{\pi}{2}\right) \sim \{1\}$ (4) $(0, 1)$
9. If $[x^2] + x - a = 0$ has a solution where $a \in \mathbb{N}$ and $a \leq 20$, then total number of 'a' can be
 (1) 2 (2) 3
 (3) 4 (4) 6
10. If $[x + [2x]] < 3$, where $[.]$ denotes the greatest integer function, then
 (1) $x \in [0, 1)$ (2) $x \in \left[-\infty, \frac{3}{2}\right)$
 (3) $x \in \left[0, \frac{3}{2}\right)$ (4) $x \in (-\infty, 1)$
11. Domain of $f(x) = \sin^{-1} [2x^3 - 3]$, where $[.]$ denotes the greatest integer function, is

(1) $\left(-\sqrt{\frac{3}{2}}, \sqrt{\frac{3}{2}}\right)$

(2) $\left[-\sqrt{\frac{3}{2}}, -1\right] \cup \left[1, \sqrt{\frac{3}{2}}\right] \cup \{1\}$

(3) $\left(-\sqrt{\frac{5}{2}}, \sqrt{\frac{5}{2}}\right)$

(4) $\left[-\sqrt{\frac{5}{2}}, -1\right] \cup \left[1, \sqrt{\frac{5}{2}}\right]$

12. If
- $y = 3[x] + 1 = 4[x - 1] - 10$
- , then
- $[x + 2y]$
- is equal to

(1) 76 (2) 61
(3) 107 (4) 67

13. Domain of
- $f(x) = \sqrt{[x] - 1 + x^2}$
- ; where
- $[.]$
- denotes the greatest integer function, is

(1) $(-\infty, -2) \cup [1, \infty)$
(2) $(-\infty, -\sqrt{2}) \cup [1, \infty)$
(3) $(-\infty, -3) \cup [1, \infty)$
(4) $(-\infty, -\sqrt{3}) \cup [1, \infty)$

14. The domain of

$$f(x) = \sqrt{\sin^{-1}(3x - 4x^3)} + \sqrt{\cos^{-1} x}$$
 is equal to

(1) $\left[-1, -\frac{\sqrt{3}}{2}\right] \cup \left[0, \frac{\sqrt{3}}{2}\right]$
(2) $\left[-1, -\frac{1}{2}\right] \cup \left[0, \frac{1}{2}\right]$
(3) $\left[0, \frac{1}{2}\right]$ (4) none of these

15. Domain of
- $f(x)$
- is
- $[-1, 2]$
- , then domain
- $f([x] - x^2 + 4)$
- where
- $[.]$
- denotes the

greatest integer function, is

(1) $[-1, \sqrt{7}]$
(2) $[-\sqrt{3}, -1] \cup [\sqrt{3}, \sqrt{7}]$
(3) $(-1, \sqrt{7})$
(4) $[-\sqrt{3}, -1] \cup [\sqrt{3}, \sqrt{7}]$

16. Range of
- $f(x) = [|\sin x| + |\cos x|]$
- , where
- $[.]$
- denotes the greatest integer function, is

(1) $\{0\}$ (2) $\{0, 1\}$
(3) $\{1\}$ (4) none of these

17. Range of
- $f(x) = \sin^{-1} x + \tan^{-1} x + \cos^{-1} x$
- is

(1) $\left(0, \frac{3\pi}{2}\right)$ (2) $\left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$
(3) $\left(-\frac{\pi}{2}, \frac{3\pi}{4}\right)$ (4) $\left(\frac{\pi}{4}, \frac{3\pi}{4}\right)$

18. Range of
- $\sin^{-1}\left[x^2 + \frac{1}{2}\right] + \cos^{-1}\left[x^2 - \frac{1}{2}\right]$

where $[.]$ denotes the greatest integer function, is

(1) $\left\{\frac{\pi}{2}, \pi\right\}$ (2) $\{\pi\}$
(3) $\left\{\frac{\pi}{2}\right\}$ (4) none of these

19. Range of
- $f(x) = \sin^{-1}\left(\sqrt{x^2 + x + 1}\right)$
- is

(1) $\left(0, \frac{\pi}{2}\right)$ (2) $\left(0, \frac{\pi}{3}\right)$
(3) $\left[\frac{\pi}{3}, \frac{\pi}{2}\right]$ (4) $\left[\frac{\pi}{6}, \frac{\pi}{3}\right]$

20. The minimum value of

$$f(x) = |x - 1| + |x - 2| + |x - 3|$$
 is equal to

(1) 1 (2) 2
(3) 3 (4) zero

21. Range of $f(x) = \frac{e^x}{[x+1]}$, $x \geq 0$ is
- (1) $(0, \infty)$ (2) $[0, \infty)$
 (3) $(1, \infty)$ (4) $[1, \infty)$
22. Range of $f(x) = [1 + \sin x] + [\cos x - 1] + [\tan^{-1} x] \forall x \in [0, 2\pi]$ is (where $[.]$ denotes the greatest integer function)
- (1) $\{-1, 1, 2\}$ (2) $\{-1, 0, 1\}$
 (3) $\{-1, 0, 1, 2\}$ (4) $\{-1, 0, 2\}$
23. Range of $f(x) = [1 + \sin x] + [2 + \sin \frac{x}{2}] + [3 + \sin \frac{x}{3}] + \dots + [n + \sin \frac{x}{n}] \forall x \in [0, \pi]$, where $[.]$ denotes the greatest integer function, is
- (1) $\left\{ \frac{n^2 + n - 2}{2}, \frac{n(n+1)}{2} \right\}$
 (2) $\left\{ \frac{n(n+1)}{2} \right\}$
 (3) $\left\{ \frac{n^2 + n - 2}{2}, \frac{n(n+1)}{2}, \frac{n^2 + n + 2}{2} \right\}$
 (4) $\left\{ \frac{n(n+1)}{2}, \frac{n^2 + n + 2}{2} \right\}$
24. $f: [-4, 4] \sim \{-\pi, 0, \pi\} \rightarrow R$, where $f(x) = \cot(\sin x) + \left[\frac{x^2}{|a|} \right]$, where $[.]$ denotes the greatest integer function, is an odd function. Complete set of values of 'a' is
- (1) $(-16, 16) \sim \{0\}$
 (2) $(-\infty, 16) \cup (16, \infty)$
 (3) $[-16, 16] \sim \{0\}$
 (4) $(-\infty, -16] \cup [16, \infty)$
25. period of $f(x) = \sin^{-1}(\sin x) + e^{\tan x}$ is
- (1) 2π (2) π
 (3) $\frac{\pi}{2}$ (4) none of these
26. Which of the following functions is non-periodic ?
- (1) $\frac{2^x}{2^{[x]}}$ (2) $\sin^{-1}(\{x\})$
 (3) $\sin^{-1}(\sqrt{\cos x})$ (4) $\sin^{-1}(\cos(x^2))$
27. If 'f' be a periodic function, then
- (1) 'f' has to be bounded
 (2) 'f' has to be onto
 (3) 'f' has to be into
 (4) 'f' may not be bounded
28. Period of $f(x) = x - [x+a] - b$, where $a, b \in R$ and $[.]$ denotes the greatest integer function, is
- (1) a (2) b
 (3) $|a-b|$ (4) 1
29. period of $f(x) = \sin 3\pi \{x\} + \tan \pi [x]$, where $[.]$ and $\{.\}$ denote the greatest integer function and fractional part respectively, is
- (1) 1 (2) 2
 (3) 3 (4) none of these
30. Period of $f(x) = [x] + [2x] + [3x] + [4x] + \dots + [nx] - \frac{n(n+1)}{2}x$ where $n \in N$, is
- (1) n (2) 1
 (3) $\frac{1}{n}$ (4) none of these
31. Total number of solutions of $2^{\cos x} = |\sin x|$ in $[-2\pi, 5\pi]$ is equal to
- (1) 12 (2) 14
 (3) 16 (4) 15

32. Let $A = \{x_1, x_2, \dots, x_m\}$, $B = \{y_1, y_2, \dots, y_n\}$, then total number of non-empty relations that can be defined from A to B, is
- (1) $m^n - 1$ (2) $n^m - 1$
 (3) $mn - 1$ (4) $2^{mn} - 1$
33. $f: R \rightarrow R$ where $f(x) = \frac{x^2 + 3x + 6}{x^2 + x + 1}$, then $f(x)$ is
- (1) many-one and into (2) many-one and onto
 (3) one-one and into (4) one-one and onto
34. $f: N \rightarrow N$ where $f(x) = x - (-1)^x$, then 'f' is
- (1) one-one and into (2) many-one and into
 (3) one-one and onto (4) many-one and onto
35. $f: R \rightarrow R$, where $f(x) = \frac{x^2 + ax + 1}{x^2 + x + 1}$, complete set of values of 'a' such that $f(x)$ is onto, is
- (1) $(-\infty, \infty)$ (2) $(-\infty, 0)$
 (3) $(0, \infty)$ (4) none of these
36. If $f(x) = \max \{x^3, x^2, \frac{1}{64}\}$ $\forall x \in [0, \infty)$, then
- (1) $f(x) = \begin{cases} x^2, & 0 \leq x \leq 1 \\ x^3, & x > 1 \end{cases}$
 (2) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{4} \\ x^2, & \frac{1}{4} < x \leq 1 \\ x^3, & x > 1 \end{cases}$
 (3) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{8} \\ x^3, & \frac{1}{8} < x \leq 1 \\ x^3, & x > 1 \end{cases}$
- (4) $f(x) = \begin{cases} \frac{1}{64}, & 0 \leq x \leq \frac{1}{8} \\ x^3, & x > \frac{1}{8} \end{cases}$
37. Total number of solutions $2^x + 3^x + 4^x - 5^x = 0$ is/are
- (1) 1 (2) 2
 (3) 3 (4) none of these
38. Let $f_1(n) = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$, then $f_1(1) + f_1(2) + f_1(3) + \dots + f_1(n)$ is equal to
- (1) $nf_1(n) - 1$ (2) $(n+1)f_1(n) - n$
 (3) $(n+1)f_1(n) + n$ (4) $nf_1(n) + n$
39. Let $f(x) = x^2 + 3x - 3$, $x \geq 0$. If n points $x_1, x_2, x_3, \dots, x_n$ are so chosen on the x-axis such that (i) $\frac{1}{n} \sum_{i=1}^n f^{-1}(x_i) = f\left(\frac{1}{n} \sum_{i=1}^n x_i\right)$
 (ii) $\frac{1}{n} \sum_{i=1}^n f^{-1}(x_i) = \sum_{i=1}^n x_i$, where f^{-1} denotes the inverse of f . then the A.M of x_i 's is
- (1) 1 (2) 2
 (3) 3 (4) 4
40. Consider a function $f(n)$ defined for all $n \in N$. The function satisfies the following two conditions
- (i) $f(1) + f(2) + f(3) + \dots \text{to } \infty = 1$.
 (ii) $f(n) = \{(1-p)p^{-1}\} \{f(n+1) + f(n+2) + \dots \text{to } \infty\}$, where $0 < p < 1$. then $f(2)$, is equal to
- (1) $p(1-p)$ (2) $1-p$
 (3) $1+p$ (4) none of these

ASSIGNMENT

1. The domain of the function

$$f(x) = {}^{24-x}C_{3x-1} + {}^{40-6x}C_{8x-10} \text{ is}$$

- (1) $\{2, 3\}$ (2) $\{1, 2, 3\}$
 (3) $\{1, 2, 3, 4\}$ (4) None of these

2. The domain of the function

$$f(x) = \cos^{-1}\left(\frac{1-|x|}{2}\right)$$

- (1) $(-\infty, -3) \cup (3, \infty)$ (2) $[-3, 3]$
 (3) $(-\infty, -3) \cup [3, \infty)$ (4) ϕ

3. The domain of the function

$$f(x) = \sqrt{e^{\sin^{-1}(\log_{16} x^2)}} \text{ is}$$

- (1) $\left[\frac{1}{4}, 4\right]$
 (2) $\left[-4, -\frac{1}{4}\right] \cup \left[\frac{1}{4}, 4\right]$
 (3) $\left[-4, -\frac{1}{4}\right]$

(4) none of these

4. The domain of the function

$$f(x) = \log_{\left[x+\frac{1}{2}\right]} |x^2 - 5x + 6| \text{ is}$$

- (1) $\left[\frac{3}{2}, 2\right) \cup (2, 3) \cup (3, \infty)$
 (2) $\left[\frac{3}{2}, \infty\right)$
 (3) $\left[\frac{1}{2}, \infty\right)$

(4) none of these

5. The domain of the function

$$f(x) = \cos^{-1}(x + [x]), \text{ where } [.] \text{ denotes the greatest integer function, is}$$

- (1) $[-1, 1]$ (2) $[0, 1]$
 (3) $(-1, 0)$ (4) none of these

6. The domain of the function

$$f(x) = \underbrace{\log_2 \log_2 \log_2 \dots \log_2 x}_{n \text{ times}} \text{ is}$$

- (1) $(2^{n-2}, \infty)$ (2) $[2^{n-2}, \infty)$
 (3) $(2^{n-2}, \infty)$ (4) none of these

7. The domain of the function

$$f(x) = \sqrt{x-3} - 3\sqrt{x-4} - \sqrt{x-3} + 2\sqrt{x-4} \text{ is}$$

- (1) $[4, \infty)$ (2) $(-\infty, 4]$
 (3) $(4, \infty)$ (4) $(-\infty, 4)$

8. The domain of the function

$$f(x) = \cos \left[\log \left(\frac{\sqrt{16-x^2}}{3-x} \right) \right] \text{ is}$$

- (1) $(-4, 4)$ (2) $(-4, 3)$
 (3) $(-\infty, -4) \cup (3, \infty)$
 (4) none of these

9. The domain of the function

$$f(x) = \frac{3+2(x+25)^{0.5}}{5-(x+25)^{0.5}} + (x-5)^{0.5} + (x-3)^{0.5} \text{ is}$$

- (1) $[5, \infty)$ (2) $[3, \infty)$
 (3) $(-25, 5)$ (4) none of these

10. The domain of the function

$$f(x) = \sqrt[4]{\log_3 \left(\frac{1}{|\cos x|} \right)} \text{ is}$$

- (1) $(-\infty, \infty)$
 (2) $(-\infty, \infty) - \{n\pi + n \in I\}$

- (3) $(-\infty, \infty) - \left\{ (2n+1)\frac{\pi}{2} : n \in I \right\}$
 (4) none of the above
11. The domain of the function $f(x) = \log_3 \left[-\log_{1/2} \left(1 + \frac{1}{x^{1/5}} \right) - 1 \right]$ is
 (1) $(-\infty, \infty)$ (2) $(0, 1)$
 (3) $(1, \infty)$ (4) none of these
12. The domain of the function $f(x) = \log_3 \left[-(\log_3 x)^2 + 5 \log_3 x - 6 \right]$
 (1) $(0, 9) \cup (27, \infty)$ (2) $[9, 27]$
 (3) $(9, 27)$ (4) none of these
13. The domain of the function $f(x) = x^{\frac{1}{\log x}}$ is
 (1) $(0, \infty) - \{1\}$ (2) $(0, \infty)$
 (3) $[0, \infty)$ (4) $[0, \infty) - \{1\}$
14. The domain of the function $f(x) = \sqrt{\frac{4-x^2}{[x]+2}}$,
 where $[x]$ denotes the greatest integer less than or equal to x , is
 (1) $[-1, 2]$ (2) $(-\infty, -2)$
 (3) $(-\infty, -2) \cup [-1, 2]$ (4) none of these
15. The domain of the function $f(x) = \log_{\left[\frac{x+1}{2} \right]} |x^2 - x - 6|$ where $[.]$ denotes the greatest integer function, is :
 (1) $\left(\frac{3}{2}, 3 \right) \cup (3, \infty)$ (2) $\left[\frac{3}{2}, 3 \right) \cup (3, \infty)$
 (3) $\left[\frac{3}{2}, 3 \right)$ (4) none of these
16. If $f(x)$ is defined on $(0, 1)$, then the domain of definition of $f(e^x) + f(\ln |x|)$ is :
 (1) $(-e, -1)$ (2) $(-e, 1)$
 (3) $(-\infty, -1) \cup (1, \infty)$ (4) $(-e, e)$
17. $f(x) = \frac{\sqrt{|\tan x| + \tan x}}{\sqrt{3x}}$ is defined for :
 (1) \mathbb{R} (2) $\mathbb{R} - \left\{ \frac{1}{3} \right\}$
 (3) $\mathbb{R} - \left\{ n\pi + \frac{\pi}{2} \mid n \in I^+ \right\}$ (4) none of these
18. The function $f(x) = \log_{10} \left(\frac{5x-x^2}{4} \right)$ exists for :
 (1) $[1, 4]$ (2) $[1, 0]$
 (3) $[0, 5]$ (4) $[5, 0]$
19. Domain of definition of the function $f(x) = \frac{3}{4-x^2} + \log_{10}(x^3 - x)$, is
 (1) $(1, 2)$
 (2) $(-1, 0) \cup (1, 2)$
 (3) $(1, 2) \cup (2, \infty)$
 (4) $(-1, 0) \cup (1, 2) \cup (2, \infty)$
20. Let $f(x) = [x]^2 + [x+1] - 3$, where $[.]$ denotes the greatest integer function, then :
 (1) $f(x) \neq 0$ for all real x
 (2) $f(x) = 0$ for only two real values
 (3) $f(x) = 0$ for infinite number of values of x
 (4) none of the above
21. Let f be a function defined on $[-2, 2]$ and is given by $f(x) = \begin{cases} -1, & -2 \leq x \leq 0 \\ x-1, & 0 < x \leq 2 \end{cases}$ and $g(x) = f(|x|) + |f(x)|$. then $g(x)$ is equal

to :

$$(1) \begin{cases} -x, & -2 \leq x < 0 \\ 0, & 0 \leq x \leq 1 \\ x-1, & 1 \leq x \leq 2 \end{cases}$$

$$(2) \begin{cases} -x, & -2 \leq x < 0 \\ 0, & 0 \leq x < 1 \\ 2(x-1), & 1 \leq x \leq 2 \end{cases}$$

$$(3) \begin{cases} -x, & -2 \leq x < 0 \\ x-1, & 0 \leq x \leq 2 \end{cases} \quad (4) \text{ none of these}$$

22. If $f(x) = \sin[\pi^2]x + \sin[-\pi^2]x$, where $[.]$ denotes the greatest integer function, then :

$$(1) f\left(\frac{\pi}{2}\right) = 1 \quad (2) f(\pi) = 2$$

$$(3) f\left(\frac{\pi}{4}\right) = 1 \quad (4) \text{ none of these}$$

23. The domain of the definition of the function $y(x)$ given by the equation $2^x + 2^y = 2$ is

$$(1) 0 < x \leq 1 \quad (2) 0 \leq x \leq 1 \\ (3) -\infty < x \leq 0 \quad (4) -\infty < x < 0$$

24. If $f(x) = \cos[\pi^2]x + \cos[-\pi^2]x$, where $[x]$ stands for the greatest integer function, then :

$$(1) f\left(\frac{\pi}{2}\right) = -1 \quad (2) f(\pi) = 1$$

$$(3) f(-\pi) = 0 \quad (4) f\left(\frac{\pi}{4}\right) = 2$$

25. The domain of definition of the function

$$f(x) = \sqrt[3]{\frac{2x+1}{x^2-10x-11}}$$
 is given by :

$$(1) x > 0 \quad (2) R - \{-1, 11\} \\ (3) x \neq -1, x \neq 11 \quad (4) -\infty < x < \infty$$

26. The domain of the function

$$f(x) = \cot^{-1}\left(\frac{x}{\sqrt{x^2 - [x^2]}}\right), x \in R \text{ is :}$$

$$(1) R - \{\pm\sqrt{n}, n \in N\}$$

$$(2) R - \{\sqrt{n}, n \geq 0, n \in N\}$$

$$(3) R \quad (4) R - \{0\}$$

27. For areal number x , $[x]$ denotes the integral part of x . The value of

$$\left[\frac{1}{2}\right] + \left[\frac{1}{2} + \frac{1}{100}\right] + \left[\frac{1}{2} + \frac{2}{100}\right] + \dots + \left[\frac{1}{2} + \frac{99}{100}\right]$$

is :

$$(1) 49 \quad (2) 50 \\ (3) 48 \quad (4) 51$$

28. The range of the function $f(x) = \sin x - \cos x$ is :

$$(1) (-\sqrt{2}, \sqrt{2}) \quad (2) [-\sqrt{2}, \sqrt{2}]$$

$$(3) [0, \sqrt{2}] \quad (4) \text{ none of these}$$

29. The range of the function $f(x) = \frac{x}{|x|}$ is

$$(1) R - \{0\} \quad (2) R - \{-1, 1\} \\ (3) \{-1, 1\} \quad (4) \text{ none of these}$$

30. The range of the function

$$f(x) = \sin\left[\log\left(\frac{\sqrt{4-x^2}}{1-x}\right)\right] \text{ is}$$

$$(1) [0, 1] \quad (2) (-1, 0) \\ (3) [-1, 1] \quad (4) (-1, 1)$$

31. The range of the function $f(x) = \frac{5}{3-x^2}$ is :

$$(1) (-\infty, 0) \cup \left[\frac{5}{3}, \infty\right) \quad (2) (-\infty, 0) \cup \left(\frac{5}{3}, \infty\right)$$

- (3) $(-\infty, 0] \cup \left[\frac{5}{3}, \infty\right)$ (4) none of these
32. The image of the interval $[1, 3]$ under the mapping
 $f: R \rightarrow R$, given by $f(x) = 2x^3 - 24x + 107$
 is :
 (1) $[0, 89]$ (2) $[75, 89]$
 (3) $[0, 75]$ (4) none of these
33. If $f(x) = \frac{x^2 - 1}{x^2 + 1}$, for every real number x ,
 then the minimum value of f :
 (1) does not exist because f is unbounded
 (2) is not attained even though f is bounded
 (3) is equal to 1 (4) is equal to -1
34. The number of values of x , where the function
 $f(x) = \cos x + \cos(\sqrt{2}x)$ attains its
 maximum, is :
 (1) 0 (2) 1
 (3) 2 (4) infinite
35. The range of the real function $\frac{x+2}{x^2-8x-4}$ is :
 (1) $\left(-\infty, -\frac{1}{4}\right] \cup \left[-\frac{1}{20}, \infty\right)$
 (2) $\left(-\infty, -\frac{1}{4}\right) \cup \left(-\frac{1}{20}, \infty\right)$
 (3) $\left(-\infty, -\frac{1}{4}\right] \cup \left(-\frac{1}{20}, \infty\right)$
 (4) none of these
36. The range of the function $f(x) = \frac{x^2 - x}{x^2 + 2x}$ is
 (1) $R / \left\{1, -\frac{1}{2}\right\}$ (2) R
 (3) $R / \{1\}$ (4) none of these
37. The range of the function
 $f(x) = \frac{x+2}{|x+2|}, x \neq -2$ is :
 (1) $\{-1, 1\}$ (2) $\{-1, 0, 1\}$
 (3) $\{1\}$ (4) $(0, \infty)$
38. The minimum value of $2^{(x^2-3)^3+27}$ is :
 (1) 1 (2) 2
 (3) 2^{27} (4) none of these
39. Let $f(x) = (1+b^2)x^2 + 2bx + 1$ and $m(b)$ the
 minimum value of $f(x)$ for a given b . As b
 varies, the range of $m(b)$ is :
 (1) $[0, 1]$ (2) $\left(0, \frac{1}{2}\right]$
 (3) $\left[\frac{1}{2}, 1\right]$ (4) $(0, 1]$
40. If f is an even function defined on the interval
 $[-5, 5]$, then the real values of x satisfying the
 equation $f(x) = f\left(\frac{x+1}{x+2}\right)$, are
 (1) $\frac{-1 \pm \sqrt{5}}{2}$ (2) $\frac{-3 \pm \sqrt{5}}{2}$
 (3) $\frac{-2 \pm \sqrt{5}}{2}$ (4) none of these
41. The function $f(x) = \sec\left[\log\left(x + \sqrt{1+x^2}\right)\right]$
 is :
 (1) even (2) odd
 (3) constant (4) non of these
42. Let the function
 $f(x) = 3x^2 - 4x + 8\log(1+|x|)$ be defined
 on the interval $[-1, 1]$ is :
 (1) $3x^2 + 4x + 8\log(1+|x|)$
 (2) $3x^2 - 4x + 8\log(1+|x|)$
 (3) $3x^2 - 4x - 8\log(1+|x|)$

- (4) none of the above
43. Which of the following functions is odd ?
 (1) $\operatorname{sgn} x + x^{2000}$ (2) $|x| - \tan x$
 (3) $x^3 \cot x$ (4) $\operatorname{cosec} x^{55}$
44. The period of the function $f(x) = \sin \sqrt{x}$ is
 (1) π (2) 2π
 (3) $\frac{\pi}{2}$ (4) none of these
45. Let $f(x) = \cos \sqrt{px}$, where $p = [a]$ = the greatest integer less than or equal to a . If the fundamental period of $f(x)$ is π , then :
 (1) $a \in [4, 5]$ (2) $a = \{4, 5\}$
 (3) $a \in [4, 5)$ (4) none of these
46. The period of the function $f(x) = \sqrt{\tan x}$ is :
 (1) π (2) 2π
 (3) $\frac{\pi}{2}$ (4) none of these
47. The period of the function $f(x) = \cos\left(\frac{8x+5}{4\pi}\right)$:
 (1) 2π (2) π
 (3) π^2 (4) none of these
48. The period of the function $f(x) = x - [x]$, where $[x]$ denotes the greatest integer less than or equal to x , is :
 (1) 2 (2) 1
 (3) 4 (4) none of these
49. If T_1 is the period of the function $y = e^{3(x-[x])}$ and T_2 is the period of the function $y = e^{3x-[3x]}$ ($[.]$ denotes the greatest integer function), then :
 (1) $T_1 = T_2$ (2) $T_1 = \frac{T_2}{3}$
 (3) $T_1 = 3T_2$ (4) none of these
50. If $e^x + e^{f(x)} = e$, then range of the function f is :
 (1) $(-\infty, 1]$ (2) $(-\infty, 1)$
 (3) $(\infty, 1)$ (4) $[1, \infty)$
51. If the period of the function $f(x) = \sin\left(\sqrt{[n]x}\right)$, where $[n]$ denotes the greatest integer less than or equal to n , is 2π , then :
 (1) $1 \leq n < 2$ (2) $1 < n < 2$
 (3) $1 \leq n \leq 2$ (4) none of these
52. The period of the function $f(x) = \cos\left(\frac{\pi x}{n!}\right) - \sin\left(\frac{\pi x}{(n+1)!}\right)$ is :
 (1) $2(n+1)!$ (2) $2(n)!$
 (3) $(n+1)$ (4) not periodic
53. The function $f(x) = k|\cos x| + k^2|\sin x| + \phi(k)$ has period $\frac{\pi}{2}$ if k is equal to :
 (1) 1 (2) 2
 (3) 3 (4) none of these
54. The period of the function $3^{(\sin^2 \pi x + x - [x] + \sin^4 \pi x)}$, where $[.]$ denotes the greatest integer function, is :
 (1) $\frac{1}{2}$ (2) 1
 (3) 2 (4) none periodic
55. The period of the function $f(x) = 2 \sin x + 3 \cos 2x$ is
 (1) π (2) 2π
 (3) $\frac{\pi}{2}$ (4) none of these
56. The period of the function $f(x) = \begin{cases} 1, & \text{when } x \text{ is a rational} \\ 0, & \text{when } x \text{ is an irrational} \end{cases}$ is

- (1) 1 (2) 2
(3) non-periodic (4) none of these
57. The period of the function $f(x) = \cos \frac{2\pi x}{5} + \sin \frac{\pi x}{4}$ is :
(1) 5 (2) 8
(3) 12 (4) 40
58. Let f be a real valued function with domain \mathbb{R} satisfying
 $f(x+k) = 1 + [2 - 5f(x) + 10\{f(x)\}^2 - 10\{f(x)\}^3 + 5\{f(x)\}^4 - \{f(x)\}^5]^{1/5}$ for all real x and some positive constant k , then the period of the function $f(x)$ is :
(1) k (2) $2k$
(3) non periodic (4) none of these
59. If the period of the function $f(x) = \tan(\sqrt{[k]x})$, where $[.]$ denotes the greatest integer function, is π , then
(1) $1 < k < 2$ (2) $1 \leq k < 2$
(3) $k = 1, 2$ (4) none of these
60. The period of the function $f(x) = \sin 5x + \cos \sqrt{3}x$ is
(1) $\sqrt{3}\pi$ (2) π
(3) non-periodic (4) none of these
61. The period of the function $f(x) = 3x + 3 - [3x + 3] + \sin \frac{\pi x}{2}$, where $[x]$ denotes the greatest integer $\leq x$, is :
(1) 4 (2) 1
(3) 2 (4) non periodic
62. The value of $n \in I$ for which the function $f(x) = \frac{\sin nx}{\sin(\frac{x}{n})}$ has 4π as its period, is :
(1) 2 (2) 3
(3) 4 (4) 5
63. π is the period of the function :
(1) $|\sin x| + |\cos x|$ (2) $\sin^4 x + \cos^4 x$
(3) $\sin(\sin x) + \sin(\cos x)$
(4) $\frac{1 + 2\cos x}{\sin x(2 + \sec x)}$
64. which of the following functions is non-periodic ?
(1) $f(x) = \tan(3x - 2)$
(2) $f(x) = \{x\}$, the fractional part of the number x
(3) $f(x) = x + \cos x$
(4) $f(x) = 1 - \frac{\cos^2 x}{1 + \tan x} - \frac{\sin^2 x}{1 + \cot x}$
65. The period of the function $f(x) = \frac{\sin 8x \cos x - \sin 6x \cos 3x}{\cos 2x \cos x - \sin 3x \sin 4x}$ is :
(1) π (2) $\frac{\pi}{2}$
(3) 2π (4) none of these
66. The period of the function $f(x) = \frac{\sin x + \sin 2x + \sin 4x + \sin 5x}{\cos x + \cos 2x + \cos 4x + \cos 5x}$ is:
(1) $\frac{\pi}{3}$ (2) $\frac{\pi}{4}$
(3) π (4) none of these
67. Let f be a real valued function with domain \mathbb{R} satisfying $0 \leq f(x) \leq \frac{1}{2}$ and for some fix a ,
 $f(x+a) = \frac{1}{2} \sqrt{f(x) - (f(x))^2} \forall x \in \mathbb{R}$,
then the period of the function $f(x)$ is
(1) a (2) $2a$
(3) non-periodic (4) none of these
68. If $f(x)$ is an odd periodic function with period 2, then $f(4)$ equals
(1) -4 (2) 4
(3) 2 (4) 0

69. If $f(x) = \sqrt{2-x}$ and $g(x) = \sqrt{1-2x}$, then the domain of $f[g(x)]$ is
- (1) $\left(-\infty, \frac{1}{2}\right]$ (2) $\left[\frac{1}{2}, \infty\right)$
 (3) $\left[-\infty, -\frac{3}{2}\right)$ (4) none of these
70. Let f be a function with domain $[-3, 5]$ and let $g(x) = |3x+4|$. Then the domain of $(f \circ g)(x)$ is
- (1) $\left(-3, \frac{1}{3}\right)$ (2) $\left[-3, \frac{1}{3}\right]$
 (3) $\left[-3, \frac{1}{3}\right)$ (4) none of these
71. If $f(x) = \frac{x-1}{x+1}$ then $f(f(ax))$ in terms of $f(x)$ is equal to
- (1) $\frac{f(x)-1}{a(f(x)+1)}$ (2) $\frac{f(x)+1}{a(f(x)-1)}$
 (3) $\frac{f(x)-1}{a(f(x)+1)}$ (4) $\frac{f(x)+1}{a(f(x)+1)}$
72. If f, g, h are function from \mathbb{R} to \mathbb{R} such that $f(x) = x^2 - 1$, $g(x) = \sqrt{x^2 + 1} \forall x \in \mathbb{R}$ and $h(x) = \begin{cases} 0, & x \leq 0 \\ x, & x \geq 0 \end{cases}$ then the composition function $h \circ (f \circ g)$ is given by
- (1) x^2 (2) 0
 (3) x (4) none of these
73. If $f(x) = \cos(\log x)$, then $f(x) \cdot f(y) - \frac{1}{2} \left\{ f\left(\frac{x}{y}\right) + f(xy) \right\}$ is equal to
- (1) 2 (2) 1 (3) 0 (4) none of these
74. If $f(x) = (3-x^7)^{1/7} \forall x \in \mathbb{R}$, then $(f \circ f)(x)$ is equal to
- (1) x (2) 0
 (3) $3-x^7$ (4) none of these
75. If $f(x) = \frac{1}{1-x}$, $g(x) = f[f(x)]$ and $h(x) = f[f\{f(x)\}]$, then the value of $f(x) \cdot g(x) \cdot h(x)$ is
- (1) 1 (2) -1
 (3) 0 (4) none of these
76. If $g[f(x)] = |\sin x|$ and $f[g(x)] = (\sin \sqrt{x})^2$, then
- (1) $f(x) = \sin^2 x, g(x) = \sqrt{x}$
 (2) $f(x) = \sin x, g(x) = |x|$
 (3) $f(x) = x^2, g(x) = \sin \sqrt{x}$
 (4) f and g cannot be determined
77. If $f(x) = |x-2|$ and $g(x) = g[f(x)]$, then for $x > 20$, $g'(x)$ is equal to
- (1) -1 (2) 1
 (3) 2 (4) none of these
78. If the function f, g, h are defined from the set of real numbers \mathbb{R} to \mathbb{R} such that $f(x) = x^2 - 1$, $g(x) = \sqrt{x^2 + 1}$, $h(x) = \begin{cases} 0, & \text{if } x \leq 0 \\ x, & \text{if } x \geq 0 \end{cases}$ then the composite function $(h \circ f \circ g)(x)$ is equal to
- (1) $\begin{cases} 0, & x=0 \\ x^2, & x>0 \\ -x^2, & x<0 \end{cases}$ (2) $\begin{cases} 0, & \text{if } x=0 \\ x^2, & \text{if } x \neq 0 \end{cases}$
 (3) $\begin{cases} 0, & x \leq 0 \\ x^2, & x > 0 \end{cases}$ (4) none of these

79. If $A = \left\{ x : -\frac{3}{5} \leq x \leq \frac{\pi-2}{5} \right\}$, $B = \{ y : -1 \leq y \leq 1 \}$
- (1) one-one but not onto
 (2) onto but not one-one
 (3) both one-one and onto
 (4) neither one-one nor onto
80. The function $f: R \rightarrow [0, 1)$, defined $f(x) = x[x]$, $\forall x \in R$ is
- (1) one-one (2) onto
 (3) both one-one and onto
 (4) neither one-one nor onto
81. The function $f: R \rightarrow R$ defined by $f(x) = 4^x + 4^{|x|}$ is
- (1) one-one and into (2) many-one and into
 (3) one-one and onto (4) many-one and onto
82. Let $f: R \rightarrow R$ be a function defined $f(x) = \frac{x^2 - 8}{x^2 + 2}$, then f is
- (1) one-one but not onto
 (2) one-one and onto
 (3) onto but not one-one
 (4) neither one-one nor onto
83. Let $f: R \rightarrow R$ be a function defined by $f(x) = x + \sqrt{x^2}$, then f is
- (1) injective (2) surjective
 (3) bijective (4) none of these
84. Let $f: (-\infty, 2] \rightarrow (-\infty, 2]$ be a function defined by $f(x) = 4x - x^2$. Then $f^{-1}(x)$ is
- (1) $2 - \sqrt{4-x}$ (2) $2 + \sqrt{4-x}$
 (3) $\sqrt{4-x}$ (4) none of these
85. Let $f: [4, \infty) \rightarrow [4, \infty)$ be a function defined by $f(x) = 5^{x(x-4)}$, then $f^{-1}(x)$ is
- (1) $2 - \sqrt{4 + \log_5 x}$ (2) $2 + \sqrt{4 + \log_5 x}$
- (3) $\left(\frac{1}{5}\right)^{x(x-4)}$ (4) none of these
86. If $f: R \rightarrow R$ is given by $f(x) = 3x - 5$, then $f^{-1}(x)$
- (1) is given by $f^{-1}(x) = \frac{1}{3x-5}$
 (2) is given by $\frac{x+5}{3}$
 (3) does not exist because f is not one-one
 (4) does not exist because f is not onto
87. Let $f: R \rightarrow R$ be given by $f(x) = (x+1)^2 - 1, x \geq -1$. Then $f^{-1}(x)$, is
- (1) $-1 + \sqrt{x+1}$ (2) $-1 - \sqrt{x+1}$
 (3) does not exist because f is not one-one
 (4) does not exist because of f is onto
88. Let $f: R \rightarrow R$ be given by $f(x) = (x+1)^2 - 1, x \geq -1$. Then, the set of values of x for which $f(x) = f^{-1}(x)$ is given by
- (1) $\{0\}$ (2) $\{0, 1\}$
 (3) $\{-1\}$ (4) none of these
89. Let $f: R \rightarrow R$ be a function defined by $f(x) = x - [x]$, where $[.]$ denotes the greatest integer function, then $f^{-1}(x)$ is
- (1) $[x] - x$ (2) $\frac{1}{x - [x]}$
 (3) not defined (4) none of these
90. The inverse of the function $y = \frac{10^x - 10^{-x}}{10^x + 10^{-x}} + 1$
- (1) $y = \frac{1}{2} \log_{10} \frac{x}{2-x}$ (2) $y = \log_{10} \frac{x}{2-x}$
 (3) $y = \frac{1}{2} \log_{10} \frac{x}{1-x}$ (4) none of these

91. The inverse of the function $f(x) = \frac{e^x - x^{-x}}{e^x + e^{-x}} + 2$ is given by
- (1) $\log_3 \left(\frac{x-1}{x+1} \right)^{-2}$ (2) $\log_e \left(\frac{x-2}{x+1} \right)^{1/2}$
- (3) $\log_e \left(\frac{x}{2-x} \right)^{1/2}$ (4) $\log_3 \left(\frac{x+1}{3-x} \right)^{1/2}$
92. Let $f: R \rightarrow R, g: R \rightarrow R$ be two functions given by $f(x) = 2x - 3, g(x) = x^3 + 5$. Then $(f \circ g)^{-1}(x)$ is equal to
- (1) $\left(\frac{x-7}{2} \right)^{1/3}$ (2) $\left(\frac{x+7}{2} \right)^{1/2}$
- (3) $\left(x - \frac{7}{2} \right)^{1/3}$ (4) $\left(\frac{x-2}{7} \right)^{1/3}$
93. $f(x+y, x-y) = xy$, then the arithmetic mean of $f(x, y)$, and $f(y, x)$ is
- (1) y (2) x
- (3) 0 (4) none of these
94. If $f(x) = 64x^3 + \frac{1}{x^3}$ and a, b are the roots of $4x + \frac{1}{x} = 3$, then:
- (1) $f(a) = 12$ (2) $f(b) = 11$
- (3) $f(a) = f(b)$ (4) none of these
95. If $3f(x) + 5f\left(\frac{1}{x}\right) = \frac{1}{x} - 3, \forall x (\neq 0) \in R$, then $f(x)$ is equal to
- (1) $\frac{1}{14} \left(\frac{3}{x} + 5x - 6 \right)$ (2) $\frac{1}{14} \left(-\frac{3}{x} + 5x - 6 \right)$
- (3) $\frac{1}{14} \left(-\frac{3}{x} + 5x + 6 \right)$ (4) none of these
96. If $f(x+y) = f(x) + f(y) - 1$ for all $x, y \in R$ and $f(1) = 1$, then the number of solutions of $f(n) = n, n \in N$ is
- (1) one (2) two
- (3) no solution (4) none of these
97. Let $f(x) = \max. \{ (1-x), (1+x), 2 \}, \forall x \in R$. Then
- (1) $f(x) = \begin{cases} 1+x, & x \leq -1 \\ 2, & -1 < x < 1 \\ 1-x, & x \geq 1 \end{cases}$
- (2) $f(x) = \begin{cases} 1-x, & x \leq -1 \\ 1, & -1 < x < 1 \\ 1+x, & x \geq 1 \end{cases}$
- (3) $f(x) = \begin{cases} 1-x, & x \leq -1 \\ 2, & -1 < x < 1 \\ 1+x, & x \geq 1 \end{cases}$
- (4) none of the above
98. The distinct linear function(s) which map(s) $[-1, 1]$ onto $[0, 2]$ is/are
- (1) $x+1, -x+1$ (2) $x-1, x+1$
- (3) $-x+1$ (4) none of these
99. If $f(x) = \frac{4^x}{4^x + 2}$, then
- $f\left(\frac{1}{1997}\right) + f\left(\frac{2}{1997}\right) + \dots + f\left(\frac{1996}{1997}\right)$ is equal to
- (1) 1997 (2) 998
- (3) 0 (4) none of these
100. The value of the natural number a for which $\sum_{k=1}^n f(a+k) = 16(2^n - 1)$, where the function f satisfies the relation $f(x+y) = f(x) \cdot f(y)$ for all natural numbers x, y and further $f(1) = 2$, is
- (1) 3 (2) 4
- (3) 2 (4) none of these

ENTRANCE CORNER

1. If X and Y are two non-empty set, where $f : X \rightarrow Y$ is function is defined such that $f(x) = \{f(x) : x \in C\}$ for, $x \subseteq X$ and $f^{-1}(D) = \{x : f(x) \in D\}$ for $D \in Y$ for any $A \subseteq X$ and $B \subseteq Y$, then
- (1) $f^{-1}(f(A)) = A$
 (2) $f^{-1}(f(A)) = A$ only if $f(x) = y$
 (3) $f(f^{-1}(B)) = B$ only if $f B \subseteq f(x)$
 (4) $f(f^{-1}(B)) = B$
2. $f(x) = \begin{cases} x, & \text{if } x \text{ is rational} \\ 0, & \text{if } x \text{ is irrational} \end{cases}$ and $g(x) = \begin{cases} 0, & \text{if } x \text{ is rational} \\ x, & \text{if } x \text{ is irrational} \end{cases}$, then fg is
- (1) one-one and into
 (2) neither one-one nor onto
 (3) many one and onto
 (4) one-one and onto
3. The second degree polynomial $f(x)$, satisfying $f(0) = 0$, $f(1) = 1$, $f'(x) > 0$ for all $x \in (0, 1)$
- (1) $f(x) = \phi$
 (2) $f(x) = ax + (1-a)x^2; \forall a \in (0, \infty)$
 (3) $f(x) = ax + (1-a)x^2, a \in (0, 2)$
 (4) no such polynomial
4. If $f(x) = \sin x + \cos x$, $g(x) = x^2 - 1$, then $f(f(x))$ is invertible in the domain
- (1) $\left[0, \frac{\pi}{2}\right]$ (2) $\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$
- (3) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ (4) $[0, \pi]$
5. Domain of definition of the function $f(x) = \sqrt{\sin^{-1}(2x) + \frac{\pi}{6}}$, for real values of x , is
- (1) $\left[-\frac{1}{4}, \frac{1}{2}\right]$ (2) $\left[-\frac{1}{2}, \frac{1}{2}\right]$
 (3) $\left[-\frac{1}{2}, \frac{1}{9}\right]$ (4) $\left[-\frac{1}{4}, \frac{1}{4}\right]$
6. Range of the function $f(x) = \frac{x^2 + x + 2}{x^2 + x + 1}; x \in \mathbb{R}$ is
- (1) $(1, \infty)$ (2) $\left(1, \frac{11}{7}\right]$
 (3) $\left(1, \frac{7}{3}\right]$ (4) $\left(1, \frac{7}{5}\right]$
7. If $f : [0, \infty) \rightarrow [0, \infty)$ and $f(x) = \frac{x}{1+x}$, then f is
- (1) one-one and onto
 (2) one-one but not onto
 (3) onto but not one-one
 (4) neither one-one nor onto
8. Suppose $f(x) = (x+1)^2$ for $x \geq -1$. If $g(x)$ is the function whose graph is the reflection of the graph of $f(x)$ with respect to the line $y = x$, then $g(x)$ equals
- (1) $-\sqrt{x} - 1, x \geq 0$ (2) $\frac{1}{(x+1)^2}, x > -1$
 (3) $\sqrt{x+1}, x \geq -1$ (4) $\sqrt{x} - 1, x \geq 0$
9. The domain of the derivative of the function

$$f(x) = \begin{cases} \tan^{-1} x, & |x| \leq 1 \\ \frac{1}{2}(|x|-1), & |x| > 1 \end{cases} \text{ is}$$

- (1) $\mathbb{R} - \{0\}$ (2) $\mathbb{R} - \{1\}$
 (3) $\mathbb{R} - \{-1\}$ (4) $\mathbb{R} - \{-1, 1\}$

10. Let the function $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by

$$f(x) = 2x + \sin x, \quad x \in \mathbb{R}. \text{ Then } f \text{ is}$$

- (1) one-one and onto
 (2) one-one but not onto
 (3) onto but not one-one
 (4) neither one-one nor onto

11. If $f: [1, +\infty) \rightarrow [2, +\infty)$ is given by

$$f(x) = x + \frac{1}{x}, \text{ then } f^{-1} \text{ equals}$$

- (1) $\frac{x + \sqrt{x^2 - 4}}{2}$ (2) $\frac{x}{1 + x^2}$
 (3) $\frac{x - \sqrt{x^2 - 4}}{2}$ (4) $1 + \sqrt{x^2 - 4}$

12. Let $E = \{1, 2, 3, 4\}$ and $F = \{1, 2\}$. Then the number of onto function from E to F is

- (1) 14 (2) 16
 (3) 12 (4) 8

13. Let $f(x) = \frac{\alpha x}{x+1}, x \neq -1$. Then for what value

$$\text{of } \alpha \text{ is } f(f(x)) = x?$$

- (1) $\sqrt{2}$ (2) $-\sqrt{2}$
 (3) 1 (4) -1

14. Let $g(x) = 1 + x - [x]$ and

$$f(x) = \begin{cases} -1, & x < 0 \\ 0, & x = 0 \\ 1, & x > 0 \end{cases}, \text{ then for all}$$

$$x, f(g(x)) \text{ is equal to}$$

- (1) x (2) 1
 (3) $f(x)$ (4) $g(x)$

15. Let $f(x) = (1 + b^2)x^2 + 2bx + 1$ and $m(b)$ the

minimum value of $f(x)$ for a given b . As b varies, the range of $m(b)$ is

- (1) $[0, 1]$ (2) $\left(0, \frac{1}{2}\right]$

- (3) $\left[\frac{1}{2}, 1\right]$ (4) $(0, 1]$

16. The domain of $f(x) = \frac{\log_2(x+3)}{x^2 + 3x + 2}$ is

- (1) $\mathbb{R} - \{-1, -2\}$ (2) $(-2, \pm\infty)$

- (3) $\mathbb{R} - \{-1, -2, -3\}$ (4) $(-3, \infty) - \{-1, -2\}$

17. Let $f(\theta) = \sin \theta (\sin \theta + \sin 3\theta)$, then $f(\theta)$ is

- (1) ≥ 0 only when $\theta \geq 0$

- (2) ≤ 0 for all real θ

- (3) ≥ 0 for all real θ

- (4) ≤ 0 only when $\theta \leq 0$

18. For all $x \in (0, 1)$

- (1) $e^x < 1 + x$ (2) $\log_e(1+x) < x$

- (3) $\sin x > x$ (4) $\log_e x > x$

19. The domain of definition of the function $y(x)$ given by $2^x + 2^y = 2$, is

- (1) $(0, 1]$ (2) $[0, 1]$

- (3) $(-\infty, 0]$ (4) $(-\infty, 1)$

20. The domain of definition of the function an interval where it is supposed to be increasing. Which of the following pairs is incorrectly matched

- | Interval | Function |
|---|-------------------------|
| (1) $(-\infty, -4)$ | $x^3 + 6x^2 + 6$ |
| (2) $\left(-\infty, \frac{1}{3}\right]$ | $3x^2 - 2x + 1$ |
| (3) $[2, \infty)$ | $2x^3 - 3x^2 - 12x + 6$ |
| (4) $(-\infty, \infty)$ | $x^3 - 3x^2 + 3x + 3$ |

21. A real valued function $f(x)$ satisfies the functional equation $f(x-y) = f(x)f(a-x)f(a+y)$ where a is a given constant and $f(0) = 1, f(2a-x)$ is equal to :
- (1) $f(-x)$ (2) $f(a) + f(a-x)$
 (3) $f(x)$ (4) $-f(x)$
22. Let $f : (-1, 1) \rightarrow B$ be a function defined by $f(x) = \tan^{-1} \frac{2x}{1-x^2}$, then f is both one-one and onto when B is the interval :
- (1) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ (2) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$
 (3) $\left[0, \frac{\pi}{2}\right)$ (4) $\left(0, \frac{\pi}{2}\right)$
23. The domain of the function $f(x) = \frac{\sin^{-1}(x-3)}{\sqrt{9-x^2}}$ is :
- (1) $[2, 3]$ (2) $[2, 3]$
 (3) $[1, 2]$ (4) $[1, 2]$
24. The graph of the function $y = f(x)$ is symmetrical about the line $x = 2$, then :
- (1) $f(x+2) = f(x-2)$
 (2) $f(2+x) = f(2-x)$
 (3) $f(x) = f(-x)$
 (4) $f(x) = -f(-x)$
25. If $f : R \rightarrow S$ defined by $f(x) = \sin x - \sqrt{3 \cos x + 1}$ is onto, then the interval of S is :
- (1) $[0, 3]$ (2) $[-1, 1]$
 (3) $[0, 1]$ (4) $[-1, 3]$
26. The range of the function $f(x) = 7^{-x} p_{x-3}$ is :
- (1) $\{1, 2, 3\}$ (2) $\{1, 2, 3, 4, 5, 6\}$
 (3) $\{1, 2, 3, 4\}$ (4) $\{1, 2, 3, 4, 5\}$
27. If $f : R \rightarrow R$ satisfies $f(x+y) = f(x) + f(y)$, for all $x, y \in R$ and $f(1) = 7$, then $\sum_{r=1}^n f(r)$ is :
- (1) $\frac{7n}{2}$ (2) $\frac{7(n+1)}{2}$
 (3) $7n(n+1)$ (4) $\frac{7n(n+1)}{2}$
28. Domain of the definition of the function $f(x) = \frac{3}{4-x^2} + \log_{10}(x^{3-x})$ is :
- (1) $(1, 2)$ (2) $(-1, 0) \cup (1, 2)$
 (3) $(1, 2) \cup (2, \infty)$
 (4) $(-1, 0) \cup (1, 2) \cup (2, \infty)$
29. The function $f(x) = \log(x + \sqrt{x^2 + 1})$ is :
- (1) an even function
 (2) an odd function
 (3) a periodic function
 (4) neither an even nor odd function
30. A function f from the set of natural numbers to integers defined by
- $$f(n) = \begin{cases} \frac{n-1}{2}, & \text{when } n \text{ is odd} \\ -\frac{n}{2}, & \text{when } n \text{ is even} \end{cases} \text{ is :}$$
- (1) one-one but not onto
 (2) onto but not one-one
 (3) one-one and onto both
 (4) neither an even nor odd function
31. The domain of $\sin^{-1} \left[\log_3 \left(\frac{x}{3} \right) \right]$ is :

- (1) $[1, 9]$ (2) $[-1, 9]$
 (3) $[-9, 1]$ (4) $[-9, -1]$
32. If $y = f(x) = \frac{x+2}{x+1}$, then
 (1) $x = f(y)$ (2) $f(1) = 3$
 (3) y increases with x for $x < 1$
 (4) f is a rational function of x
33. If $f(x) = \cos(\log x)$,
 then $f(x)f(y) - \frac{1}{2} \left[f\left(\frac{x}{y}\right) + f(xy) \right]$ has
 the value :
 (1) -1 (2) $\frac{1}{2}$
 (3) -2 (4) none of these
34. If $f(x) = x^2 + 1$, then
 $f^{-1}(17)$ and $f^{-1}(13)$ will be :
 (1) 4, 1 (2) 4, 0
 (3) 3, 2 (4) none of these
35. Inverse of the function $y = 2x - 3$ is :
 (1) $\frac{x+3}{2}$ (2) $\frac{x-3}{2}$
 (3) $\frac{1}{2x-3}$ (4) none of these
36. If x is real then value of the expression
 $\frac{x^2 + 14x + 9}{x^2 + 2x + 3}$ lies between ;
 (1) 5 and 4 (2) 5 and -4
 (3) -5 and 4 (4) none of these
37. Let $f: R \rightarrow R$ be a function defined by
 $f(x) = \frac{x-m}{x-n}$, where $m \neq n$. then :
 (1) f is one-one onto
 (2) f is one-one into
 (3) f is many-one onto
 (4) f is many-one into
38. Set A has 3 elements and set B has 4 elements.
 The number of injection that can be defined
 from A to B is
 (1) 144 (2) 12
 (3) 24 (4) 64
39. If $f(x) = a \cos(bx + c) + d$, then range of
 $f(x)$ is :
 (1) $[d+a, d+2a]$ (2) $[a-d, a+d]$
 (3) $[d+a, a-d]$ (4) $[d-a, d+a]$
40. Domain of the function
 $f(x) = \left[\log_{10} \left(\frac{5x-x^2}{4} \right) \right]^{1/2}$ is :
 (1) $-\infty < x < \infty$ (2) $1 \leq x \leq 4$
 (3) $4 \leq x \leq 16$ (4) $-1 \leq x \leq 1$
41. If $f(x) = ax + b$ and $g(x) = cx + d$, then
 $f(g(x)) = g(f(x))$ is equal to :
 (1) $f(a) = g(c)$ (2) $f(b) = g(b)$
 (3) $f(d) = g(b)$ (4) $f(c) = g(a)$
42. If $f(x) = 3x + 10$, $g(x) = x^2 - 1$, then
 $(f \circ g)^{-1}$ is equal to :
 (1) $\left(\frac{x-7}{3} \right)^{1/2}$ (2) $\left(\frac{x+7}{3} \right)^{1/2}$
 (3) $\left(\frac{x-3}{7} \right)^{1/2}$ (4) $\left(\frac{x+3}{7} \right)^{1/2}$
43. If $f(x) = \cos^2 x + \sec^2 x$, then :
 (1) $f(x) < 1$ (2) $f(x) = 1$
 (3) $2 > f(x) > 1$ (4) $f(x) \geq 2$
44. The composite mapping fog of the map
 $f: R \rightarrow R$, $f(x) = \sin x$, $g: R \rightarrow R$,
 $g(x) = x^2$ is :
 (1) $\sin x + x^2$ (2) $(\sin x)^2$

45. Which of the statements given below is different from others ?
- (1) $f : A \rightarrow B$ (2) $f : x \rightarrow f(x)$
 (3) f is a mapping of A into B
 (4) none of these
46. The domain of $\sin^{-1}[\log_3(x/3)]$ is :
- (1) $[1,9]$ (2) $[-1,9]$
 (3) $[-9,1]$ (4) $[-9,-1]$
47. The domain of definition of the function $f(x) = \sqrt{\log_{10}\left(\frac{5x-x^2}{4}\right)}$ is :
- (1) $[1,4]$ (2) $[1,0]$
 (3) $[0,5]$ (4) $[5,0]$
48. Let $f : (2,3) \rightarrow (0,1)$ be defined by $f(x) = x - [x]$, then $f^{-1}(x)$ equals :
- (1) $x-2$ (2) $x+1$
 (3) $x-1$ (4) $x+2$
49. $f(x) = ax^2 + bx + c$ and $g(x) = px^2 + qx$ with $g(1) = f(1)$, $g(2) - f(2) = 1$, $g(3) - f(3) = 4$, then $g(4) - f(4)$ is :
- (1) 0 (2) 5
 (3) 6 (4) none of these
50. Range of the function $f(x) = \frac{x^2}{x^2+1}$ is :
- (1) $(-1,0)$ (2) $(-1,1)$
 (3) $[0,1)$ (4) $(1,1)$
51. The period of the function $\sin\left(\frac{2x}{3}\right) + \sin\left(\frac{3x}{2}\right)$ is :
- (1) 2π (2) 10π
 (3) 6π (4) 12π
52. $f(x) = x + \sqrt{x^2}$ is a function from \mathbb{R} to \mathbb{R} , then $f(x)$ is :
- (1) injective (2) surjective
 (3) bijective (4) none of these
53. Let $f(x) = \sin(\log x)$, then the value of $f(xy) + f\left(\frac{x}{y}\right) - 2f(x)\cos(\log y)$ is :
- (1) -1 (2) 0
 (3) 2 (4) 1
54. The function $f(x) = \frac{1 - \sin x + \cos x}{1 + \sin x + \cos x}$ is not defined at $x = \pi$, is :
- (1) $-\frac{1}{2}$ (2) $\frac{1}{2}$
 (3) -1 (4) 1
55. The function defined by $f(x) = \begin{cases} \left(x^2 + e^{\frac{1}{2-x}}\right)^{-1}, & x \neq 2 \\ k, & x = 2 \end{cases}$ is continuous from right at the point $x = 2$, then k is equal to :
- (1) 0 (2) $1/4$
 (3) $-1/4$ (4) none of these
56. If $f(x) = \cot^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$ and $g(x) = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$, then $\lim_{x \rightarrow a} \frac{f(x) - f(a)}{g(x) - g(a)}$, $0 < a < \frac{1}{2}$ is :
- (1) $\frac{3}{2(1+a^2)}$ (2) $\frac{3}{2(1+x^2)}$
 (3) $\frac{3}{2}$ (4) $-\frac{3}{2}$

57. Let $A = R - \{3\}$, $B = R - \{1\}$, let $f : A \rightarrow B$ be defined by $f(x) = \frac{x-2}{x-3}$, then :
- (1) f is bijective
 - (2) f is one-one but not onto
 - (3) f is onto but not one-one
 - (4) none of these
58. The domain of the function $f(x) = {}^{16-x}C_{2x-1} + {}^{20-3x}P_{4x-5}$, where the symbols have their usual meanings, is the set:
- (1) $\{2, 3\}$
 - (2) $\{2, 3, 4\}$
 - (3) $\{1, 2, 3, 4\}$
 - (4) $\{1, 2, 3, 4, 5\}$
59. If $y = f(x) = \frac{ax+b}{cx-a}$, then x is equal to :
- (1) $1/f(x)$
 - (2) $1/f(y)$
 - (3) $yf(x)$
 - (4) $f(y)$
60. If $f(x+ay, x-ay) = axy$, then $f(x, y)$ is equal to :
- (1) xy
 - (2) $x^2 - a^2y^2$
 - (3) $\frac{x^2 - y^2}{4}$
 - (4) $\frac{x^2 - y^2}{a^2}$
61. The domain of the function $y = \sqrt{\frac{1}{x} - 1}$ is :
- (1) $x \leq 1$
 - (2) $0 \leq x \leq 1$
 - (3) $0 \leq x < 1$
 - (4) $0 < x \leq 1$
62. The period of $f(x) = x - [x]$, if it is periodic, is :
- (1) $f(x)$ is not periodic
 - (2) $\frac{1}{2}$
 - (3) 1
 - (4) 2
63. Let $f : N \rightarrow N$ defined by $f(x) = x^2 + x + 1, x \in N$, then f is
- (1) one-one onto
 - (2) many- one onto
 - (3) one-one but not onto
 - (4) non of these
64. Let $f(x) = ax + b$ and $g(x) = cx + d, a \neq 0, c = 0$. assume $a = 1, b = 2$. If $(f \circ g)(x) = (g \circ f)(x)$ for all x , what can you say about c and d ?
- (1) c and d both are arbitrary
 - (2) $c = 1, d$ is arbitrary
 - (3) c is arbitrary, $d = 1$
 - (4) $c = 1, d = 1$
65. Which of the following function is inverse function ?
- (1) $f(x) = \frac{1}{x-1}$
 - (2) $f(x) = x^2$, for all x
 - (3) $f(x) = x^2, x \geq 0$
 - (4) $f(x) = x^2, x \leq 0$
66. The largest possible set of real numbers which can be the domain of $f(x) = \sqrt{1 - \frac{1}{x}}$, is :
- (1) $(0, 1) \cup (0, \infty)$
 - (2) $(-1, 0) \cup (1, \infty)$
 - (3) $(-\infty, -1) \cup (0, \infty)$
 - (4) $(-\infty, 0) \cup (1, \infty)$
67. If $f(x)$ is periodic function with period T , then the function $f(ax+b)$ where $a > 0$, is periodic with period :
- (1) T/b
 - (2) aT
 - (3) bT
 - (4) T/a
68. Domain of $f(x) = \log |\log x|$ is :
- (1) $(0, \infty)$
 - (2) $(1, \infty)$
 - (3) $(0, 1) \cup (1, \infty)$
 - (4) $(-\infty, 1)$
69. The domain of the function $f(x) = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$ is :
- (1) $] -3, -2.5[\cup] -2.5, -2[$
 - (2) $[-2, 0[\cup] 0, 1[$
 - (3) $] 0, 1[$
 - (4) none of these

70. If $f : R \rightarrow R$ is defined by $f(x) = [2x] - 2[x]$ for $x \in R$, where $[x]$ is the greatest integer not exceeding x , then the range of f is:

- (1) $\{x \in R : 0 \leq x \leq 1\}$ (2) $\{0, 1\}$
 (3) $\{x \in R : x > 0\}$ (4) $\{x \in R : x \leq 0\}$

71. If $f : R \rightarrow R$ is defined by

$$f(x) = \begin{cases} x+4 & \text{for } x < -4 \\ 3x+2 & \text{for } -4 \leq x < 4 \\ x-4 & \text{for } x \geq 4 \end{cases} \text{ then the}$$

correct matching of List from List II is
 List - I List - II

- | | | | |
|-------------------------|------------|-----------|---------|
| (1) $f(-5) + f(-4)$ | (i) 14 | | |
| (2) $f(f(-8))$ | (ii) 4 | | |
| (3) $f(f(-7) + f(3))$ | (iii) -11 | | |
| (4) $f(f(f(f(0)))) + 1$ | (iv) -1 | | |
| | (v) 1 | | |
| | (vi) 0 | | |
| (1) (iii) | (2) (vi) | (3) (ii) | (4) (v) |
| (2) (iii) | (4) (iv) | (ii) (v) | |
| (3) (iv) | (iii) (ii) | (i) (i) | |
| (4) (iii) | (vi) (v) | (ii) (ii) | |

72. If $f : R \rightarrow R$ is defined by $f(x) = x - [x] - \frac{1}{2}$ for $x \in R$, where $[x]$ is the greatest integer not exceeding x , then

$$\left\{x \in R : f(x) = \frac{1}{2}\right\} \text{ is equal to}$$

- (1) Z , the set of all integers
 (2) N , the set of all natural numbers
 (3) ϕ , the empty set
 (4) R

73. The function $f : C \rightarrow C$ defined by

$$f(x) = \frac{ax+b}{cx+d} \text{ for } x \in C \text{ where } bd \neq 0$$

reduces to a constant function, if :

- (1) $a = c$ (2) $b = d$
 (3) $ad = bc$ (4) $ab = cd$

74. If N denotes the set of all positive integers and if $f : N \rightarrow N$ is defined by $f(n) =$ the sum of positive divisors of n then, $f(2^k, 3)$, where k is a positive integers, is

- (1) $2^{k+1} - 1$ (2) $2(2^{k+1} - 1)$
 (3) $3(2^{-k+1} - 1)$ (4) $4(2^{k+1} - 1)$

75. If $f : R \rightarrow R$ and $g : R \rightarrow R$ are given by $f(x) = |x|$ and $g(x) = [x]$ for each $x \in R$, then

$$\{x \in E : g(f(x)) \leq f(g(x))\} \text{ is equal to}$$

- (1) $I \cup (-\infty, 0)$ (2) $(-\infty, 0)$
 (3) I (4) R

76. Suppose $f : [2, 2] \rightarrow R$ is defined by

$$f(x) = \begin{cases} -1, & \text{for } -2 \leq x \leq 0 \\ x-1, & \text{for } 0 \leq x \leq 2 \end{cases}, \text{ then}$$

$$\{x \in \{-2, 2\} : x \leq 0 \text{ and } f(|x|) = x\} \text{ is equal to}$$

- (1) $\{-1\}$ (2) $\{0\}$
 (3) $\{-1/2\}$ (4) ϕ

77. If $f : R \rightarrow R$ and $g : R \rightarrow R$ are defined by $f(x) = 2x + 3$ and $g(x) = x^2 + 7$, then the values of x such $g(f(x)) = 8$ are

- (1) 1, 2 (2) -1, 2
 (3) -1, -2 (4) 1, -2

78. If $e^{f(x)} = \frac{10+x}{10-x}, x \in (-10, 10)$ and

$$f(x) = kf\left(\frac{200x}{100+x^2}\right), \text{ then } k \text{ is equal to}$$

- (1) 0.5 (2) 0.6
 (3) 0.7 (4) 0.8

79. If $f(x) = \frac{1}{\sqrt{x+2}\sqrt{2x-4}} + \frac{1}{\sqrt{x-2}\sqrt{2x-4}}$,
for $x > 2$, then $f(11)$ is equal to
- (1) $\frac{7}{6}$ (2) $\frac{5}{6}$
(3) $\frac{6}{7}$ (4) $\frac{5}{7}$
80. The function $f: R \rightarrow R$ is defined by
 $f(x) = \cos^2 x + \sin^4 x$ for $x \in R$, then
 $f(R)$ is equal to
- (1) $\left[\frac{3}{4}, 1\right]$ (2) $\left[\frac{3}{4}, 1\right)$
(3) $\left[\frac{3}{4}, 1\right)$ (4) $\left(\frac{3}{4}, 1\right)$
81. If $f(x) = \frac{\cos^2 x + \sin^4 x}{\sin^2 x + \cos^4 x}$ for $x \in R$, then
 $f(2002)$ equal to
- (1) 1 (2) 2
(3) 3 (4) 4
82. If $f: R \rightarrow R$ be defined by $f(x) = 2x + 3$ and
 $g(x) = x^2 + 7$, then the value of x for which
 $f(g(x)) = 25$ are
- (1) ± 1 (2) ± 2
(3) ± 3 (4) ± 4
83. Let $f: R \rightarrow R$ be defined by
 $f(x) = 2x + |x|$, then
 $f(2x) + f(-x) - f(x)$ is equal to
- (1) $2x$ (2) $2|x|$
(3) $-2x$ (4) $-2|x|$
84. Let X and Y be subsets of R , the set of the real
numbers. The function $F: X \rightarrow Y$ defined by
 $f(x) = x^2$ for $x \in X$ is one-one but not onto
- (1) $X = Y = R^+$ (2) $X = r, Y = R^+$
(3) $X = R^+, Y = R$ (4) $X = Y = R$
85. The range of the function $f(x) = \frac{x+2}{|x+2|}$ is
- (1) $\{0, 1\}$ (2) $\{-1, 1\}$
(3) R (4) $R - \{-2\}$
86. The domain of the function
 $f(x) = \sin^{-1}[\log_2(x/2)]$ is
- (1) $[1, 4]$ (2) $[-4, 1]$
(3) $[-1, 4]$ (4) none of these
87. The range of $f(x) = \cos(x/3)$ is
- (1) $(-1/3, 1/3)$ (2) $[-1, 1]$
(3) $\{1/3, -1/3\}$ (4) $(-3, 3)$
88. The domain of the function
 $f(x) = \log(\sqrt{x-4} + \sqrt{6-x})$ is
- (1) $[4, \infty)$ (2) $(-\infty, 6]$
(3) $[4, 6]$ (4) none of these
89. The inverse of the function $\frac{10^x - 10^{-x}}{10^x + 10^{-x}}$ is
- (1) $\frac{1}{2} \log_{10} \left(\frac{1+x}{1-x} \right)$ (2) $\frac{1}{2} \log_{10} \left(\frac{1-x}{1+x} \right)$
(3) $\frac{1}{4} \log_{10} \left(\frac{2x}{2-x} \right)$ (4) none of these
90. The domain of the function
 $f(x) = \sqrt{\log \frac{1}{|\sin x|}}$ is
- (1) $R - \{2n\pi, n \in I\}$ (2) $R - \{n\pi, n \in I\}$
(3) $R - \{-\pi, \pi\}$ (4) $(-\infty, \infty)$
91. If $f: R \rightarrow R$, then $f(x) = |x|$ is
- (1) one-one but not onto
(2) onto but not one-one
(3) one-one and onto
(4) none of these
92. If $f(x) = \frac{\alpha x}{x+1}, x \neq -1$ for what value of α
is $f(f(x)) = x$?

- (1) $\sqrt{2}$ (2) $-\sqrt{2}$
 (3) 1 (4) 2
93. The domain of $\sin^{-1}(\log_3 x)$ is
 (1) $[-1, 1]$ (2) $[0, 1]$
 (3) $[0, \infty]$ (4) \mathbb{R}
 (5) $\left[\frac{1}{3}, 3\right]$
94. The function f satisfies the functional equation
 $3f(x) + 2f\left(\frac{x+59}{x-1}\right) = 10x + 30$ for all real
 $x \neq 1$. The value of $f(7)$ is
 (1) 8 (2) 4
 (3) -8 (4) 11
 (5) 44
95. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by
 $f(x) = x^2 - 6x - 14$, then $f^{-1}(2)$ equals to
 (1) $\{2, 8\}$ (2) $\{-2, 8\}$
 (3) $\{-2, -8\}$ (4) $\{2, -8\}$
 (5) $\{\emptyset\}$
96. Let $f: \mathbb{R} \rightarrow \mathbb{R}: f(x) = x^2$ and
 $g: \mathbb{R} \rightarrow \mathbb{R}: g(x) = x + 5$, then $g \circ f$ is
 (1) $(x+5)$ (2) $(x+5)^2$
 (3) (x^2+5^2) (4) $(x+5)^2$
 (5) (x^2+5)
97. The range of the function \sin
 $(\sin^{-1} x + \cos^{-1} x)$, $|x| \leq 1$ is
 (1) $[-1, 1]$ (2) $[1, -1]$
 (3) $\{0\}$ (4) $\{-1\}$
 (5) $\{1\}$
98. If $f(x) = \cos(\log_e x)$, then
 $f(x)f(y) - \frac{1}{2}\left[f\left(\frac{y}{x}\right) + f(xy)\right]$ has the
 value
 (1) 1 (2) $1/2$
 (3) -2 (4) 0
 (5) -1
99. Domain of the function $f(x) = \sin^{-1}(\log_2 x)$
 in the set of real numbers, is
 (1) $\{x: 1 \leq x \leq 2\}$ (2) $\{x: 1 \leq x \leq 3\}$
 (3) $\{x: -1 \leq x \leq 2\}$ (4) $\left\{x: \frac{1}{2} \leq x \leq 2\right\}$
 (5) $\left\{x: -\frac{1}{2} \leq x \leq 2\right\}$
100. If $f(x) = \frac{1-x}{1+x}$, ($x \neq -1$), then $f^{-1}(x)$
 equals to
 (1) $f(x)$ (2) $1/f(x)$
 (3) $-f(x)$ (4) $-1/f(x)$
 (5) not defined
101. Let the function f be defined by
 $f(x) = \frac{2x+1}{1-3x}$, then $f^{-1}(x)$ is:
 (1) $\frac{x-1}{3x+2}$ (2) $\frac{3x+2}{x-1}$
 (3) $\frac{x+1}{3x-2}$ (4) $\frac{2x+1}{1-3x}$
102. If $f(x) = \log \frac{1+x}{1-x}$, then $f(x)$ is:
 (1) even function
 (2) $f(x_1)f(x_2) = f(x_1+x_2)$
 (3) $\frac{f(x_1)}{f(x_2)} = f(x_1-x_2)$
 (4) odd function
103. which one of the following is a bijective function
 on the set of real number?
 (1) $2x-5$ (2) $|x|$
 (3) x^2 (4) x^2+1

104. If $f(x) = \frac{2x+1}{3x-2}$, then $(f \circ f)(2)$ is equal to :
- (1) 1 (2) 3
(3) 4 (4) 2
105. If $f(x)$ is a function such that $f^{-1}(x) + f(x) = 0$ and $g(x) = [f(x)]^2 + [f'(x)]^2$ and $g(3) = 3$ then $g(8)$ is equal to :
- (1) 5 (2) 0
(3) 3 (4) 8
106. If $f(x)$ and $g(x)$ are two functions with $g(x) = x - \frac{1}{x}$ and $f \circ g(x) = x^3 - \frac{1}{x^3}$, then $f'(x)$ is:
- (1) $3x^2 + 3$ (2) $x^2 - \frac{1}{x^2}$
(3) $1 + \frac{1}{x^2}$ (4) $3x^2 + \frac{3}{x^4}$
107. The function $f : x \rightarrow y$ defined by $f(x) = \sin x$ is one-one but not onto, if X and Y are respectively equal to :
- (1) R and R (2) $[0, \pi]$ and $[0, 1]$
(3) $\left[0, \frac{\pi}{2}\right]$ and $[-1, 1]$
(4) $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ and $[-1, 1]$
108. If R denotes the set of all real numbers, then the function $f : R \rightarrow R$ defined $f(x) = |x|$ is :
- (1) one-one only (2) onto only
(3) both one-one and onto
(4) neither one-one nor onto
109. The function $f : R \rightarrow R$ defined by $f(x) = e^x$ is :
- (1) onto (2) many-one
(3) one-one and into (4) many-one and onto
110. If the function $f(x)$ is defined by $f(x) = a + bx$ and $f^r = f \circ f \circ \dots$ (repeated r times), then $f^r(x)$ is equal to :
- (1) $a + b^r x$ (2) $ar + b^r x$
(3) $ar + bx^r$ (4) $a \left(\frac{b^r - 1}{b - 1} \right) + b^r x$
111. $f(x) = \frac{1-x}{1+x}$ ($x \neq -1$), then $f^{-1}(x)$ equals to :
- (1) $f(x)$ (2) $\frac{1}{f(x)}$
(3) $-f(x)$ (4) $-\frac{1}{f(x)}$
112. If $2f(x+1) + f\left(\frac{1}{x+1}\right) = 2x$ and $x \neq -1$, then $f(2)$ is equal to :
- (1) -1 (2) 2
(3) 5/3 (4) 5/2
113. If $f(x) = \frac{2x-2}{x+5}$, ($x \neq 5$), then $f^{-1}(x)$ is equal to :
- (1) $\frac{x+5}{2x-1}$, $x \neq \frac{1}{2}$ (2) $\frac{5x+1}{2-x}$, $x \neq 2$
(3) $\frac{x-5}{2x-1}$, $x \neq -\frac{1}{2}$ (4) $\frac{5x-1}{2-x}$, $x \neq 2$
114. If $f(x) = \frac{x}{x-1}$, then $\underbrace{(f \circ f \circ \dots \circ f)}_{19 \text{ times}}(x)$ is equal to :
- (1) $\frac{x}{(x-1)}$ (2) $\left(\frac{x}{x-1}\right)^{19}$
(3) $\frac{19x}{(x-1)}$ (4) x

115. The domain of the function

$$f(x) \exp(\sqrt{5x-3-2x^2}) \text{ is}$$

(1) $[3/2, \infty)$ (2) $[1, 3/2]$

(3) $(-\infty, 1]$ (4) $(1, 3/2)$

116. If 'n' is an integer, then domain of the function

$$\sqrt{\sin 2x} \text{ is:}$$

(1) $\left[n\pi - \frac{\pi}{2}, n\pi \right]$ (2) $\left[n\pi, n\pi + \frac{\pi}{2} \right]$

(3) $\left[(2n-1)\pi, 2n\pi \right]$ (4) $\left[2n\pi, (2n+1)\pi \right]$

117. The domain of the function

$$\sqrt{\log(x^2 - 6x + 5)} \text{ is:}$$

(1) $(-\infty, \infty)$

(2) $(-\infty, 3 - \sqrt{3}) \cup (3 + \sqrt{3}, \infty)$

(3) $(-\infty, 1] \cup [5, \infty)$

(4) $[0, \infty)$

118. Suppose that $g(x) = 1 + \sqrt{x}$ and

$$f(g(x)) = 3 + 2\sqrt{x+x}, \text{ then } f(x) \text{ is:}$$

(1) $1 + 2x^2$ (2) $2 + x^2$

(3) $1 + x$ (4) $2 + x$